



**CORRECTION OF MAIN RING QUADRUPOLE POSITIONS  
USING CLOSED ORBIT INFORMATION**

G. McD. Bingham

January 5, 1970

Abstract

The computer program OTRIM is described and results are presented for some simple cases. The program calculates corrections to be applied to the transverse positions of the Main Ring quadrupoles. The input data consists of a set of measurements of the transverse position of the closed orbit relative to the quadrupoles -- the beam sensor readings. The basic program assumes one beam sensor for each transverse direction at each Main Ring station i.e.  $\sim$  one beam sensor for each transverse direction per quadrupole. An arbitrary beam sensor configuration may be introduced simply by specifying, in the input data, the numbers of the beam sensors of the basic configuration which are inoperative. The results of some simple misalignment cases indicate that, in principle, OTRIM can reduce the closed orbit deviation by factors  $\sim 10^8$  when all beam sensors are operative. With 10% of the beam sensors inoperative, the maximum reduction factor ranges from  $\sim 20-40$  (inoperative beam sensors arbitrarily distributed) to  $<2$  (inoperative beam sensors are consecutive). The case in which there are beam sensors at only the F quadrupoles in a given plane was also considered in order to obtain an indication of the loss of correction power in the event that it was desired to halve



the system cost. The results for this case indicate a maximum correction factor  $\sim 20-40$ . While this factor is probably adequate, it must be noted that, in actual practice, it will be further reduced by inoperative beam sensors, by errors in the beam sensor readings and the position corrections applied to the quadrupoles, and perhaps by non-linear effects. Thus it is rather doubtful if the halved system would be adequate in actual practice.

### Introduction

The position of the closed orbit with respect to the beam elements of a synchrotron is determined by the magnetic fields and the positions of the beam elements. In this report we will show how errors in the positioning of the beam elements may be reduced by knowledge of the closed orbit position at a number of points around the accelerator -- the beam sensor readings. Since there are more beam elements than beam sensors in the present case, we cannot hope to uniquely remove a given position error.

The Main Ring of the NAL 200 GeV accelerator has six superperiods and uses a separated function lattice. The most critical alignment requirements are for the transverse (horizontal, i.e. radial; vertical) location of the quadrupoles. Thus the errors in the transverse location of the quadrupoles are the only beam element position errors that we consider. Laslett has calculated<sup>1</sup> that the quadrupoles must be located with an accuracy of .01 in. in these directions for a 75%

probability that the corresponding closed orbit deviation is contained within a width of 1 in.

The positioning of the quadrupoles may be considered to be achieved in three steps -

(a) Construction survey in which the quadrupoles are located using the station markers<sup>2</sup> which were placed to an accuracy  $\sim 1/16$  in. during construction.

(b) Refined survey using precise levels, tapes and an alignment laser. The wire alignment system described in the NAL Design Report has recently been discarded. The refined survey will probably be done one lattice cell at a time. Its accuracy should be such as to achieve a circulating beam.

(c) Final positioning of the quadrupoles using the beam sensor readings as described in this report. This same correction scheme may be used to relocate the quadrupoles if the closed orbit happened to move during the life of the accelerator.

### Theory

In Figure 1 is shown the arrangement for the first of the six superperiods of the Main Ring. There are 14 standard cells (C) a half cell (DF), a medium straight cell (CM) and a one half cell replacement containing the long straight section (FLD). The parameters for all of these cells are taken from the report by Garren<sup>3</sup>. Small changes to the FLD section were made by Bellendir and Teng<sup>4</sup> during the progress of this work. They have not been included.

The following notation is used in reference to the complete Main Ring -  $B(I)$ ,  $I = 1, 210$  - the beam sensors which measure the closed orbit displacement relative to the appropriate beam element. This information is then used to correct the quadrupole positions. It is assumed that a beam sensor is located at each station marker, including the one at the center of the long straight section.

$Y(I)$ ,  $I = 1, 210$  - the spy station beam sensors. This information is not used to correct the quadrupole positions. Its sole use is to enable us to investigate the remaining closed orbit deviations at points intermediate to the  $B(I)$  after the quadrupole positions have been corrected. In the present case the spy stations are somewhat academic as we would not expect their readings to differ significantly from those of the beam sensors  $B(I)$  because of the small separation between  $B(I)$  and  $Y(I)$ .

$H(I)$ ,  $I = 1, 222$  - the transverse displacement of the  $I$ th beam element. From Figure 1 we note that the  $I = 2, 3, 36, 37$ , etc., elements are quadrupole doublets whereas the remaining elements are singlets. The main reason for this choice of beam elements is to obtain a program which does not exceed the available space in present large computers (CDC 6600, IBM 360/75).

Because of the small separation between members of the above doublets, the assumption of no relative displacement of the members is probably quite accurate. Notice also from Figure 1 that there is no quadrupole associated with  $H(1)$ ,  $H(38)$  etc.

In this report we use the correction scheme which has been described by Laslett and Lambertson<sup>5</sup>. We define the matrix S with the equation

$$B = S H \quad (1)$$

where B and H are given by

$$B = \begin{pmatrix} B(1) \\ B(2) \\ \vdots \\ B(NB) \end{pmatrix} \quad \text{i.e. column matrix of beam sensor readings, NB = 210 here}$$

$$H = \begin{pmatrix} H(1) \\ H(2) \\ \vdots \\ H(NH) \end{pmatrix} \quad \text{i.e. column matrix of displacement of accelerator components. NH = 222 here}$$

We assume that the horizontal plane motion is not coupled to that of the vertical plane. Thus the two directions are computed independently and each has its own S matrix. The S matrices are computed by the program SYNCH<sup>6</sup> and the details of this computation are given in Appendix 1. For the combined function machine that they considered, Laslett and Lambertson found it convenient to displace the beam elements in gangs rather than individually. Thus if G is the ganging matrix for the gang scheme chosen, we have

$$B = TH \quad (2)$$

where  $T = SG$ . Although we only consider individual displacements ( $G = 1$ ), our calculations are set up so that any desired G matrix may be introduced.

In practice we will be faced with the situation where the B matrix is given by a set of beam sensor readings and we wish to find the set of displacement corrections  $H_C$  which are to be applied in order to give a zero B matrix. Ideally we would invert (2) and obtain

$$H_C = -H = -T^{-1} B \quad (3)$$

In general T is not square and so the above step is not possible. Furthermore, it is not possible even when T is a square matrix because B contains only relative beam displacements and thus a unique  $H_C$  does not exist, i.e. T has a zero value determinant. Thus it is necessary to use a different approach from that of Eqn. (3). From Eqn. (2) we have

$$\bar{B} T = \bar{H} \bar{T} T \quad (4)$$

where  $\bar{B}$  is the transpose of B, etc. Laslett and Lambertson show that Eqn. (4) also results if one fits the beam sensor readings by least squares. We define the matrix M by

$$M = \bar{T} T \quad (5)$$

Thus M is a symmetric matrix with either zero or positive eigenvalues. If the Kth eigenvalue and normalized eigenvector are respectively  $\lambda^K$  and  $V^K$  we have

$$M V^K = \lambda^K V^K \quad (6)$$

We then expand H in terms of the  $V^L$

$$H = \sum_L A_L V^L \quad (7)$$

By multiplying Eqn. (4) by  $V^K$  from the right and using Eqns. (5), (6), (7) we obtain

$$A_K = \frac{\bar{B}^T V^K}{\lambda^K} \quad (8)$$

Next we define the Q matrix from

$$\bar{H}_C = -\bar{H} = \bar{B} Q \quad (9)$$

Thus from Eqns. (7), (8), (9) we have

$$Q = -\sum_L \frac{T V^L \bar{V}^L}{\lambda^L} \quad (10)$$

Laslett and Lambertson also note that the sum of squares of the beam sensor readings is given by

$$\sum_I B^2(I) = \bar{B}B = \sum_L \lambda^L A_L^2 \quad (11)$$

i.e. the component of this sum due to the Lth eigenvector is proportional to  $\lambda^L$ . Thus Eqn. (11) shows that the small eigenvalues and their eigenvectors can be dropped from the sum over L in Eqn. (10) (of course, the  $\lambda=0$  ones must be dropped) and the result will not be greatly affected. This is the key point of the Laslett and Lambertson method. They found that dropping the small eigenvalue eigenvectors from the Q sum reduced the closed orbit deviation at points intermediate to the beam sensors in some cases. This effect should not be large in our case as we have  $\sim 1$  beam sensor per quadrupole. They also found that the total amount of corrective displacement was significantly reduced as small eigenvalue eigenvectors were omitted. In practice we calculate several Q matrices and investigate the behavior of  $H_C$  as the number of omitted eigenvectors is varied.

### Computer Program OTRIM

The computer program OTRIM performs the computation of the displacement corrections  $H_c$  to be applied to the quadrupoles from a given set of beam sensor readings B. The program uses two magnetic tapes. Tape 3 is the input tape (read only) containing the SYNCH output and obtained as set out in Appendix 1. Tape 4 is a scratch tape (both read and write).

The input data sets required are as shown at the top of Figure 2 and will be described here in detail --

First Set (1 card only) Format (16I5). This is the program instruction card and contains, in order, the input values for the following variables:

ITEST = 0 - beam sensor readings to be input with punched cards

= 1 - run test case for which only non-zero displacement is  $H(2) = +1.0$  and beam sensor readings are obtained by OTRIM from SYNCH output (Tape 3).

ISPY = 0 - skip spy stations

= 1 - calculate closed orbit displacement at spy stations after corrections  $H_c$  have been applied to beam elements. It is run only for test case, ITEST = 1.

NHOR = 0 - skip horizontal plane

= 1 - run horizontal plane



NVERT = 0 - skip vertical plane  
          = 1 - run vertical plane

KAPUTH       - the number of inoperative beam sensors for  
                  the horizontal plane.

KAPUTV       - the number of inoperative beam sensors  
                  for the vertical plane.

NVCHEK = 0 - skip orthogonality test on eigenvectors of  $\bar{T}T$ .  
          = 1 - perform orthogonality test.

NHARM = 0 - skip the harmonic analysis of GV.  
          = 1 - perform the harmonic analysis of GV.

NNNQ        - the number of Q matrices which are to be  
                  calculated. This number must be sufficiently  
                  small to allow them to be written on the  
                  scratch tape (Tape 4). Using NNNQ = 6 re-  
                  quires that Tape 4 be 2400 feet with density  
                  800 b.p.i. This resulted in frequent parity  
                  errors so we have usually taken NNNQ = 5  
                  and 556 b.p.i.

Second Set   Format (16I5)   KAP(J), J=1, KAPUTH. The identi-  
fication numbers of the beam sensors which are inoperative  
(i.e. no available reading) in the horizontal plane.

Third Set   Format (16I5)   NQ(J), J=1, NNNQ. The numbers of  
small non-zero eigenvalue eigenvectors that are to be dropped  
from the horizontal plane Q matrices. These numbers must be  
arranged in descending order. For NB<NH (our case) the  
smallest NQ(J) may be NQ(NNNQ)=0. However, if NB=NH, the  
smallest allowable NQ(J) is NQ(NNNQ)=1 (see later).

TM-200

0402

Fourth Set Format (8F10.4) BS(J), J=1, NB. The beam sensor readings for the horizontal plane. The number fields of inoperative beam sensors remain blank. For test case runs (ITEST=1) no BS(J) data set is required as OTRIM obtains the appropriate data from the SYNCH output.

<u>Fifth Set</u> Format (16I5) KAP(J), J=1, KAPUTV	} vertical plane data
<u>Sixth Set</u> Format (16I5) NQ(J), J=1, NNNQ	
<u>Seventh Set</u> Format (8F10.4) BS(J), J=1, NB	

When both horizontal and vertical planes are to be computed, the order of the input data must be as above. If only one plane is to be computed, the input data consists of the instruction card and the three sets corresponding to that plane.

A listing of OTRIM is contained in Appendix 2 of this report. The operation of the program is outlined by the flow diagram in Figure 2. The program begins by reading into the columns of a matrix SY either the horizontal plane or the vertical plane SYNCH output, according to the instruction card. The SYNCH output gives the absolute displacements of the closed orbit for the sequential displacement of the first superperiod quadrupoles by 1 unit. The SYNCH displacement sequence is shown in Figure 1. We require the displacement of the closed orbit relative to the beam elements - i.e. the beam sensor readings. Also we must include matrix elements corresponding to the beam sensors at the center of the long straight sections. Thus OTRIM sets up the required S matrix

as follows -

$$\begin{aligned}
 S(1,1) &= -1. \\
 S(I,1) &= 0. & I = 2, NB & \left. \vphantom{S(I,1)} \right\} (12) \\
 S(I,J) &= SY(I,J-1) & I = 1, NB \text{ but } I \neq 2. & J = 2,3 \left. \vphantom{S(I,J)} \right\} (13) \\
 S(I,J) &= SY(I,J-1) - 0.5 & I = 2. & J = 2,3 \left. \vphantom{S(I,J)} \right\} \\
 S(I,J) &= SY(I,J-1) & I = 1, NB \text{ but } I \neq J-1. & J = 4,35 \left. \vphantom{S(I,J)} \right\} (14) \\
 S(I,J) &= SY(I,J-1) - 1.0 & I = J-1 & J = 4,35 \left. \vphantom{S(I,J)} \right\} \\
 S(I,J) &= SY(I,J-1) & I = 1, NB \text{ but } I \neq 35. & J = 36,37 \left. \vphantom{S(I,J)} \right\} (15) \\
 S(I,J) &= SY(I,J-1) - 0.5 & I = 35. & J = 36,37 \left. \vphantom{S(I,J)} \right\}
 \end{aligned}$$

Eqn. (12) gives the elements corresponding to the beam sensor at the center of the long straight section. In Eqn. (13) it has been assumed that the displacement of beam sensor B(2) is given by  $1/2 (H(2) + H(3))$ . A similar assumption is made for B(35) in Eqn. (15). The remaining beam sensors are assumed to be fixed to the adjacent quadrupoles - Eqn. (14). Eqns. (12), (13), (14), (15) set up 1/6 of the S matrix. The remaining 5/6 of this matrix is obtained by cyclic symmetry

$$S(I + \frac{N}{6} \times NB, J + \frac{N}{6} \times NH) = S(I, J) \quad (16)$$

with N an integer. The indices I and J are modulo NB and NH respectively.

OTRIM next proceeds to calculate the matrix  $T=SG$ . We have simply used  $G=1$  in this work, but any desired ganging matrix may be introduced at this point. Since we measure only relative displacement of the closed orbit, the displacement of all beam elements uniformly by 1 unit (horizontally or vertically) should produce no change in the closed orbit.

Thus the program checks for zero sum of the elements of each row of the T matrix. In fact the sums for the vertical direction may be  $\sim 1 \times 10^{-2}$  due to slight vertical focussing at the entrance and exit planes of the bending magnets.

The inoperative beam sensors KAP(J) are allowed as the next step in the computation. The corresponding rows are dropped from the T matrix and the resulting reduced matrix is the R matrix. The matrix  $M = \bar{R}R$  is then computed. KAP(I), T and M are all stored on the scratch tape for subsequent use.

The non-zero eigenvalues and their associated eigenvectors are computed and arranged in descending order by the subroutine EIGEN<sup>7</sup> for the matrix M. If NR is the number of rows in R and  $NR < NH$  (the present case) then the number of non-zero eigenvalues is NR. Thus the arguments of EIGEN are set up so as to compute for the NR largest eigenvalues. If we had a case where  $NR = NH$ , then the last of the NR eigenvalues computed would be zero (see below Eqn. 3). Thus for the  $NR = NH$  case the minimum value for NQ (NNNQ) is 1.

If NVCHEK = 1, then subroutine VCHEK checks that the eigenvectors of M are orthonormal using the equations

$$\begin{aligned} \bar{V}^I M V^J &= \lambda^J & I &= J \\ &= 0 & I &\neq J \end{aligned} \quad (17)$$

The subroutine assigns a limit of  $(10^{-10} + 2 \times 10^{-8} \lambda^J)$  to the difference between left and right sides of Eqn. (17). Typically  $\sim 10\%$  of the smaller eigenvectors fall outside this limit by  $\sim 10^{-9}$  and this is considered quite satisfactory.

TM-200  
0402

If NHARM = 1, subroutine HAR will perform the harmonic analysis of  $GV^L$ . For each non-zero eigenvector, OTRIM lists the four largest amplitudes and their frequencies. In the present case the harmonic analysis is unreliable and should be omitted because it assumes equal argument increments whereas in fact the  $H(I)$  are spaced as shown in Figure 1. The harmonic behavior of the Main Ring is best understood by studying its harmonic response as shown in Appendix 3.

OTRIM is now ready to compute the NNNQ Q matrices which involve the omission or various numbers NQ of small eigenvalue eigenvectors. For reasons of computer economy the program calculates one column of all NNNQ Q matrices and stores these NNNQ columns as a record on Tape 4. It then proceeds to the next column of all Q matrices, and so on, until all NNNQ Q matrices are complete.

Each Q matrix is then read back from Tape 4 and the program computes the recommended displacement corrections HQ (equivalent to  $H_c$ ) from Eqn. (9) and the total correction motion HQTOT.

$$HQTOT = \sum |HQ| \quad (18)$$

For the test case the residual beam sensor readings BE are computed

$$BE = T (H+HQ) \quad (19)$$

Also for the test case the subroutine NUMBER computes the maximum beam sensor reading, the r.m.s. beam sensor reading and the r.m.s. value of the local maxima of beam sensor

TM-200  
0402

reading. These parameters are computed both before and after application of HQ so that the improvement may be noted.

If ISPY = 1 and the test case is being run, OTRIM will proceed to compute, for each Q matrix, the residual displacement of the closed orbit relative to the beam elements at the spy stations, i.e. the residual beam sensor readings at the spy stations, BSP. Referring to Eqn. (1), we now have B replaced by Y and it is necessary to set up the corresponding spy S matrix. It is assumed that the spy station sensors are fixed to the adjacent quadrupoles. Thus the procedure is similar to that in Eqns. (12)-(15) except that in the present case there is no beam sensor whose motion is determined by the motion of two quadrupoles as in Eqns. (13) and (15). Also the spy S matrix is set up directly in the SY array into which the spy SYNCH data has been read (beginning in column 2) as the S array of OTRIM contains data which is required later. Thus the equations are

$$\left. \begin{aligned} SY(I,J) &= 0. & I = 1, \text{ NB. } J = 1 \\ SY(I,J) &= SY(I,J) - 1. & I = 1, \quad J = 2 \\ SY(I,J) &= SY(I,J) - 1. & I = J - 2, \quad J = 4, 37 \end{aligned} \right\} (20)$$

All other elements in the first 1/6 of SY will be correct as read in. The remaining 5/6 of the matrix is obtained by cyclic symmetry and then the BSP values are computed.

OTRIM has now completed the computation for the plane in which it started. If this plane was the horizontal plane and NVERT = 1, then it returns to compute for the vertical plane. Otherwise, the computation is complete and the program ends.

## Results

(a) No inoperative beam sensors, NKAPUT = 0

In Figure 3 we have plotted the displacement in both planes of the accelerator components before and after correction for the test case  $H(2) = +1.0$ . Only the components near  $H(2)$  are shown for two  $Q$  matrices ( $NQ=0$  and  $NQ=108$ ) which correspond to the omission of 0 and 108 non-zero small eigenvalue eigenvectors. As  $NQ$  is reduced, the maximum residual error is reduced and the accelerator components are placed on a smooth bump relative to the undisplaced positions. At most, the bump extends over  $\sim$  one superperiod near the displaced element. The remainder of the accelerator is unchanged.

Figure 4 shows the variation in both planes of maximum beam sensor reading| after correction, as  $NQ$  is changed. The initial displacements are also shown. The general trend is for a reduced residual beam sensor reading as  $NQ$  is reduced. For  $NQ = 0$ , the residual beam sensor readings are only  $\sim 10^{-8}$ . Even when  $NQ = 108$  (i.e. slightly more than half the eigenvectors are omitted) it is still possible to reduce the closed orbit deviation by a factor  $\sim 10$ . The variation of  $HQTOT$  with  $NQ$  is shown in Figure 5. It is seen that  $HQTOT$  may increase by a factor  $\sim 2-3$  as  $NQ$  is reduced over the range shown.

As will be discussed later (Appendix 3) it is important that OTRIM is able to correct 20th harmonic (integer closest to  $\nu$ ) disturbances. Figures 6, 7, and 8 show the results when

the 20th harmonic disturbance extended  $\sim 1$  wavelength. As NQ is reduced the beam elements are moved from their disturbed positions on to a small smooth bulge. Residual beam sensor readings  $\sim 10^{-8}$  are theoretically possible in this case also. In Figure 8 we see that HQTOT tends to oscillate about the initial sum, first increasing and then decreasing as HQ is reduced.

Figures 9 and 10 present results for a disturbance of  $\sim 1$  wavelength of 40th harmonic. They indicate that smaller (factor 2-4) residual beam sensor readings are possible, but otherwise are similar to 20th harmonic case.

(b) 96 inoperative beam sensors, NKAPUT = 96

This case is interesting because it indicates whether we can hope to obtain sufficient information by placing beam sensors for a given plane at only the focussing quadrupoles for that plane, i.e. where the beam width function is a maximum. Such a scheme would represent a large financial saving. It is in contrast to (a) above where each beam sensor actually consists of a pair, one for the horizontal plane and one for the vertical plane. In the present case we have assumed that both horizontal plane and vertical plane beam sensors exist at B1, B2, B35, B36, B37, etc. Otherwise beam sensors exist only at QF quadrupoles in the plane of interest.

The results have been plotted in Figures 11 and 12 for the test case  $H(2) = +1.0$ . It is seen that the reduction in



closed orbit deviation is now only  $\sim$  factor 20-40 in the most favorable case. Also the trend as NO is varied is not monotonic for small values of NQ. Thus it may be necessary to choose somewhat larger NQ values (and consequently a smaller reduction of closed orbit deviation) in an actual case. It is seen from Figure 12 that HQTOT tends to decrease slightly as NQ is reduced to small values  $\sim 10$ . For further reduction of NQ HQTOT may increase slightly in some cases.

(c) 21 inoperative beam sensors, NKAPUT = 21

In this case we have returned to case (a) and imagined that 10% of the beam sensors are inoperative. This is an attempt to represent an actual situation since at any given time there will probably exist some inoperative beam sensors - say 10%. We chose 21 inoperative beam sensors in an arbitrary way and the results are plotted in Figures 13 and 14. It is seen that both the maximum residual beam sensor reading and HQTOT are rather slowly varying with NQ. The maximum reduction in closed orbit deviation is  $\sim$  factor 40 now and so the correction is much poorer than in the case (a).

Also shown in Figures 13 and 14 is the case 21 consecutive inoperative beam sensors for the horizontal plane. As might be expected, this is a severe loss of information and OTRIM is only able to reduce the closed orbit deviation by  $\sim 20\%$ .

#### Discussion

Although we have considered only a few misalignment examples, these examples are important as Lambertson and Laslett

found that the single misaligned quadrupole case was the most difficult to correct. Also the 20th harmonic is expected to be the most important misalignment harmonic (Appendix 3). In the present accelerator, these misalignments can be largely corrected by OTRIM even when a significant fraction of the beam sensors are inoperative. This difference in behavior is probably due to the fact that with the present separated function machine there is  $\sim 1$  beam sensor per focussing magnet whereas with the combined function machine of Lambertson and Laslett there was only  $\sim 1$  beam sensor per 7 focussing magnets. For the same reason, in the present case the spy stations do not show residual deviations that are much different from the residual deviations at the beam sensors. Also in our work there does not appear to be excessive total component displacement HQTOT as NQ is reduced. The residual beam sensor error is usually much smaller as NQ is reduced. Although it would be desirable to consider more misalignment examples, at present there appears to be no reason for not choosing NQ=0.

The question of whether it is sufficient to use beam sensors at only the QF quadrupoles of a given plane requires some further study before a definite answer may be given. The present work indicates that the closed orbit can still be corrected by a factor  $\sim 20-40$ , which would probably be adequate. However, it must be noted that the above correction factor will be reduced when allowance is made for --

#### 1. Inoperative beam sensors

2. Errors in beam sensor readings
3. Errors in position corrections applied to beam elements
4. Non-linear effects (if there are any?)

Thus it appears rather doubtful that it will be adequate to use beam sensors at only the QF quadrupoles. While such an arrangement may halve the cost of the beam sensor system, it reduces the maximum possible closed orbit correction by orders of magnitude.

### Acknowledgements

We are indebted to A.A. Garren, G.R. Lambertson and L. Jackson Laslett for discussions of this work and assistance with the programs. Burton S. Garbow was most helpful in the eigenvalue - eigenvector computations. Most of the computer runs were made remotely at N.Y.U. and we wish to acknowledge the assistance of the N.A.L. Computer Center staff, especially Miss A. Georgoulakis.

### References

1. N.A.L. Design Report, p5-20, January, 1968.  

The estimate is contained in a letter from Dr. Laslett to Dr. Wilson, dated December 21, 1967. It was obtained for the horizontal direction and assumed that the quadrupoles were located horizontally by making offset measurements relative to a polygon of 200 sides. Only the errors in the offset measurements were considered. The estimate then follows from a formula derived by L. Jackson Laslett and Lloyd Smith in UCID-10161, p 17. The same estimate applies for the vertical direction if we assume that, in the vertical direction also, the displacement errors of individual quadrupoles are uncorrected.
2. T.L. Collins, TS-2, 1968.
3. A.A. Garren, FN-182 0400 March 12, 1969.
4. J. Bellendir and L.C. Teng, FN-189 0420 May 21, 1969.
5. G.R. Lambertson and L. Jackson Laslett, Proceedings, V International Conference on High Energy Accelerators, Frascati, 1965 (C.N.E.N., Rome, 1966) pp. 26-33. Also same authors, Proceedings of VI International Conference on High Energy Accelerators, Cambridge, 1967. pp. 226-227.
6. A.A. Garren and J.W. Eusebio, SYNCH, A Computer System for Synchrotron Design and Orbit Analysis, Lawrence Radiation Laboratory Report UCID-10153, April 10, 1965.
7. Burton S. Garbow, ANL F202S, System/360 Library Subroutine,

TM-200  
0402

Applied Mathematics Division, Argonne National Laboratory,  
December, 1967; Revised, June 1968. The subroutine is  
set up for easy conversion to CDC 6600 use.

8. L. Jackson Laslett, AS/Accelerator Systems/03, July 14,  
1965 and September 20, 1966.

Appendix 1 SYNCH Input Data

The lattice used is that described by Garren<sup>3</sup>. The input is set up for the system of beam sensors and spy stations shown in Figure 1. The elements of the first superperiod are displaced 1 unit in sequence. For each of these displacements SYNCH calculates the position of the closed orbit, in addition to other parameters, at all beam sensors and spy stations around the accelerator. The output which is written on the output Tape 5 under the format (A5, 2I3, 5F14.8) is as follows -

Name of Matrix                    (RING in our case)  
Number of the beam sensor or spy station, n. (1-420)  
Total number of beam sensors and spy stations (420)  
Distance from beginning to n  
Closed orbit position, horizontal plane, at n  
Closed orbit position, vertical plane, at n  
Horizontal beta function at n  
Vertical beta function at n

The desired SY matrix is then obtained by using appropriate read formats in OTRIM. In the case we have considered, Tape 5 was 2400 ft. long and 556 b.p.i.

[illegible]

00U  
LML  
LLHA  
LLA  
AA3

05X  
00S  
A23  
A21  
LLB  
LLM  
LLG  
GGD  
BRH  
BB  
QQF  
QGD  
OF  
FF  
QD  
FL  
GD  
BL

X  
2  
1  
B  
M  
G  
D  
H  
  
8  
L  
\*  
\*  
\*  
\*

[illegible]

USX IS SENSOR DIST. FROM QUAD, VDRM CELL USX+OOSX=00

1. 31953  
 2. 736336  
 3. 31953  
 4. 31953  
 5. 31953  
 6. 31953  
 7. 31953  
 8. 31953  
 9. 31953  
 10. 31953  
 11. 31953  
 12. 31953  
 13. 31953  
 14. 31953  
 15. 31953  
 16. 31953  
 17. 31953  
 18. 31953  
 19. 31953  
 20. 31953  
 21. 31953  
 22. 31953  
 23. 31953  
 24. 31953  
 25. 31953  
 26. 31953  
 27. 31953  
 28. 31953  
 29. 31953  
 30. 31953  
 31. 31953  
 32. 31953  
 33. 31953  
 34. 31953  
 35. 31953  
 36. 31953  
 37. 31953  
 38. 31953  
 39. 31953  
 40. 31953  
 41. 31953  
 42. 31953  
 43. 31953  
 44. 31953  
 45. 31953  
 46. 31953  
 47. 31953  
 48. 31953  
 49. 31953  
 50. 31953  
 51. 31953  
 52. 31953  
 53. 31953  
 54. 31953  
 55. 31953  
 56. 31953  
 57. 31953  
 58. 31953  
 59. 31953  
 60. 31953  
 61. 31953  
 62. 31953  
 63. 31953  
 64. 31953  
 65. 31953  
 66. 31953  
 67. 31953  
 68. 31953  
 69. 31953  
 70. 31953  
 71. 31953  
 72. 31953  
 73. 31953  
 74. 31953  
 75. 31953  
 76. 31953  
 77. 31953  
 78. 31953  
 79. 31953  
 80. 31953  
 81. 31953  
 82. 31953  
 83. 31953  
 84. 31953  
 85. 31953  
 86. 31953  
 87. 31953  
 88. 31953  
 89. 31953  
 90. 31953  
 91. 31953  
 92. 31953  
 93. 31953  
 94. 31953  
 95. 31953  
 96. 31953  
 97. 31953  
 98. 31953  
 99. 31953  
 100. 31953

Misaligned  
Quadruples.

T(I) ARE FIXED MATRICES; ALSO XL, FX, DX NORMAL CELLS  
 P(I) ARE MATRICES VARIED (FIRST SUPERPERIOD)  
 S(I) ARE SHIFT MATRICES



XLX  
T1  
T2  
T3  
T4  
T5  
T6  
T7  
T8  
T9  
T10  
T11  
T12  
T13  
T14  
T15  
T16  
T17  
T18  
T19  
T20  
T21  
T22  
T23  
T24  
T25  
T26  
T27  
T28  
T29  
T30  
T31  
T32  
T33  
T34  
T35  
T36  
T37  
T38  
T39  
T40  
T41  
T42  
T43  
T44  
T45  
T46  
T47  
T48  
T49  
T50  
T51  
T52  
T53  
T54  
T55  
T56  
T57  
T58  
T59  
T60  
T61  
T62  
T63  
T64  
T65  
T66  
T67  
T68  
T69  
T70  
T71  
T72  
T73  
T74  
T75  
T76  
T77  
T78  
T79  
T80  
T81  
T82  
T83  
T84  
T85  
T86  
T87  
T88  
T89  
T90  
T91  
T92  
T93  
T94  
T95  
T96  
T97  
T98  
T99  
T100  
T101  
T102  
T103  
T104  
T105  
T106  
T107  
T108  
T109  
T110  
T111  
T112  
T113  
T114  
T115  
T116  
T117  
T118  
T119  
T120  
T121  
T122  
T123  
T124  
T125  
T126  
T127  
T128  
T129  
T130  
T131  
T132  
T133  
T134  
T135  
T136  
T137  
T138  
T139  
T140  
T141  
T142  
T143  
T144  
T145  
T146  
T147  
T148  
T149  
T150  
T151  
T152  
T153  
T154  
T155  
T156  
T157  
T158  
T159  
T160  
T161  
T162  
T163  
T164  
T165  
T166  
T167  
T168  
T169  
T170  
T171  
T172  
T173  
T174  
T175  
T176  
T177  
T178  
T179  
T180  
T181  
T182  
T183  
T184  
T185  
T186  
T187  
T188  
T189  
T190  
T191  
T192  
T193  
T194  
T195  
T196  
T197  
T198  
T199  
T200  
T201  
T202  
T203  
T204  
T205  
T206  
T207  
T208  
T209  
T210  
T211  
T212  
T213  
T214  
T215  
T216  
T217  
T218  
T219  
T220  
T221  
T222  
T223  
T224  
T225  
T226  
T227  
T228  
T229  
T230  
T231  
T232  
T233  
T234  
T235  
T236  
T237  
T238  
T239  
T240  
T241  
T242  
T243  
T244  
T245  
T246  
T247  
T248  
T249  
T250  
T251  
T252  
T253  
T254  
T255  
T256  
T257  
T258  
T259  
T260  
T261  
T262  
T263  
T264  
T265  
T266  
T267  
T268  
T269  
T270  
T271  
T272  
T273  
T274  
T275  
T276  
T277  
T278  
T279  
T280  
T281  
T282  
T283  
T284  
T285  
T286  
T287  
T288  
T289  
T290  
T291  
T292  
T293  
T294  
T295  
T296  
T297  
T298  
T299  
T300  
T301  
T302  
T303  
T304  
T305  
T306  
T307  
T308  
T309  
T310  
T311  
T312  
T313  
T314  
T315  
T316  
T317  
T318  
T319  
T320  
T321  
T322  
T323  
T324  
T325  
T326  
T327  
T328  
T329  
T330  
T331  
T332  
T333  
T334  
T335  
T336  
T337  
T338  
T339  
T340  
T341  
T342  
T343  
T344  
T345  
T346  
T347  
T348  
T349  
T350  
T351  
T352  
T353  
T354  
T355  
T356  
T357  
T358  
T359  
T360  
T361  
T362  
T363  
T364  
T365  
T366  
T367  
T368  
T369  
T370  
T371  
T372  
T373  
T374  
T375  
T376  
T377  
T378  
T379  
T380  
T381  
T382  
T383  
T384  
T385  
T386  
T387  
T388  
T389  
T390  
T391  
T392  
T393  
T394  
T395  
T396  
T397  
T398  
T399  
T400  
T401  
T402  
T403  
T404  
T405  
T406  
T407  
T408  
T409  
T410  
T411  
T412  
T413  
T414  
T415  
T416  
T417  
T418  
T419  
T420  
T421  
T422  
T423  
T424  
T425  
T426  
T427  
T428  
T429  
T430  
T431  
T432  
T433  
T434  
T435  
T436  
T437  
T438  
T439  
T440  
T441  
T442  
T443  
T444  
T445  
T446  
T447  
T448  
T449  
T450  
T451  
T452  
T453  
T454  
T455  
T456  
T457  
T458  
T459  
T460  
T461  
T462  
T463  
T464  
T465  
T466  
T467  
T468  
T469  
T470  
T471  
T472  
T473  
T474  
T475  
T476  
T477  
T478  
T479  
T480  
T481  
T482  
T483  
T484  
T485  
T486  
T487  
T488  
T489  
T490  
T491  
T492  
T493  
T494  
T495  
T496  
T497  
T498  
T499  
T500  
T501  
T502  
T503  
T504  
T505  
T506  
T507  
T508  
T509  
T510  
T511  
T512  
T513  
T514  
T515  
T516  
T517  
T518  
T519  
T520  
T521  
T522  
T523  
T524  
T525  
T526  
T527  
T528  
T529  
T530  
T531  
T532  
T533  
T534  
T535  
T536  
T537  
T538  
T539  
T540  
T541  
T542  
T543  
T544  
T545  
T546  
T547  
T548  
T549  
T550  
T551  
T552  
T553  
T554  
T555  
T556  
T557  
T558  
T559  
T560  
T561  
T562  
T563  
T564  
T565  
T566  
T567  
T568  
T569  
T570  
T571  
T572  
T573  
T574  
T575  
T576  
T577  
T578  
T579  
T580  
T581  
T582  
T583  
T584  
T585  
T586  
T587  
T588  
T589  
T590  
T591  
T592  
T593  
T594  
T595  
T596  
T597  
T598  
T599  
T600  
T601  
T602  
T603  
T604  
T605  
T606  
T607  
T608  
T609  
T610  
T611  
T612  
T613  
T614  
T615  
T616  
T617  
T618  
T619  
T620  
T621  
T622  
T623  
T624  
T625  
T626  
T627  
T628  
T629  
T630  
T631  
T632  
T633  
T634  
T635  
T636  
T637  
T638  
T639  
T640  
T641  
T642  
T643  
T644  
T645  
T646  
T647  
T648  
T649  
T650  
T651  
T652  
T653  
T654  
T655  
T656  
T657  
T658  
T659  
T660  
T661  
T662  
T663  
T664  
T665  
T666  
T667  
T668  
T669  
T670  
T671  
T672  
T673  
T674  
T675  
T676  
T677  
T678  
T679  
T680  
T681  
T682  
T683  
T684  
T685  
T686  
T687  
T688  
T689  
T690  
T691  
T692  
T693  
T694  
T695  
T696  
T697  
T698  
T699  
T700  
T701  
T702  
T703  
T704  
T705  
T706  
T707  
T708  
T709  
T710  
T711  
T712  
T713  
T714  
T715  
T716  
T717  
T718  
T719  
T720  
T721  
T722  
T723  
T724  
T725  
T726  
T727  
T728  
T729  
T730  
T731  
T732  
T733  
T734  
T735  
T736  
T737  
T738  
T739  
T740  
T741  
T742  
T743  
T744  
T745  
T746  
T747  
T748  
T749  
T750  
T751  
T752  
T753  
T754  
T755  
T756  
T757  
T758  
T759  
T760  
T761  
T762  
T763  
T764  
T765  
T766  
T767  
T768  
T769  
T770  
T771  
T772  
T773  
T774  
T775  
T776  
T777  
T778  
T779  
T780  
T781  
T782  
T783  
T784  
T785  
T786  
T787  
T788  
T789  
T790  
T791  
T792  
T793  
T794  
T795  
T796  
T797  
T798  
T799  
T800  
T801  
T802  
T803  
T804  
T805  
T806  
T807  
T808  
T809  
T810  
T811  
T812  
T813  
T814  
T815  
T816  
T817  
T818  
T819  
T820  
T821  
T822  
T823  
T824  
T825  
T826  
T827  
T828  
T829  
T830  
T831  
T832  
T833  
T834  
T835  
T836  
T837  
T838  
T839  
T840  
T841  
T842  
T843  
T844  
T845  
T846  
T847  
T848  
T849  
T850  
T851  
T852  
T853  
T854  
T855  
T856  
T857  
T858  
T859  
T860  
T861  
T862  
T863  
T864  
T865  
T866  
T867  
T868  
T869  
T870  
T871  
T872  
T873  
T874  
T875  
T876  
T877  
T878  
T879  
T880  
T881  
T882  
T883  
T884  
T885  
T886  
T887  
T888  
T889  
T890  
T891  
T892  
T893  
T894  
T895  
T896  
T897  
T898  
T899  
T900  
T901  
T902  
T903  
T904  
T905  
T906  
T907  
T908  
T909  
T910  
T911  
T912  
T913  
T914  
T915  
T916  
T917  
T918  
T919  
T920  
T921  
T922  
T923  
T924  
T925  
T926  
T927  
T928  
T929  
T930  
T931  
T932  
T933  
T934  
T935  
T936  
T937  
T938  
T939  
T940  
T941  
T942  
T943  
T944  
T945  
T946  
T947  
T948  
T949  
T950  
T951  
T952  
T953  
T954  
T955  
T956  
T957  
T958  
T959  
T960  
T961  
T962  
T963  
T964  
T965  
T966  
T967  
T968  
T969  
T970  
T971  
T972  
T973  
T974  
T975  
T976  
T977  
T978  
T979  
T980  
T981  
T982  
T983  
T984  
T985  
T986  
T987  
T988  
T989  
T990  
T991  
T992  
T993  
T994  
T995  
T996  
T997  
T998  
T999  
T1000  
T1001  
T1002  
T1003  
T1004  
T1005  
T1006  
T1007  
T1008  
T1009  
T1010  
T1011  
T1012  
T1013  
T1014  
T1015  
T1016  
T1017  
T1018  
T1019  
T1020  
T1021  
T1022  
T1023  
T1024  
T1025  
T1026  
T1027  
T1028  
T1029  
T1030  
T1031  
T1032  
T1033  
T1034  
T1035  
T1036  
T1037  
T1038  
T1039  
T1040  
T1041  
T1042  
T1043  
T1044  
T1045  
T1046  
T1047  
T1048  
T1049  
T1050  
T1051  
T1052  
T1053  
T1054  
T1055  
T1056  
T1057  
T1058  
T1059  
T1060  
T1061  
T1062  
T1063  
T1064  
T1065  
T1066  
T1067  
T1068  
T1069  
T1070  
T1071  
T1072  
T1073  
T1074  
T1075  
T1076  
T1077  
T1078  
T1079  
T1080  
T1081  
T1082  
T1083  
T1084  
T1085  
T1086  
T1087  
T1088  
T1089  
T1090  
T1091  
T1092  
T1093  
T1094  
T1095  
T1096  
T1097  
T1098  
T1099  
T1100  
T1101  
T1102  
T1103  
T1104  
T1105  
T1106  
T1107  
T1108  
T1109  
T1110  
T1111  
T1112  
T1113  
T1114  
T1115  
T1116  
T1117  
T1118  
T1119  
T1120  
T1121  
T1122  
T1123  
T1124  
T1125  
T1126  
T1127  
T1128  
T1129  
T1130  
T1131  
T1132  
T1133  
T1134  
T1135  
T1136  
T1137  
T1138  
T1139  
T1140  
T1141  
T1142  
T1143  
T1144  
T1145  
T1146  
T1147  
T1148  
T1149  
T1150  
T1151  
T1152  
T1153  
T1154  
T1155  
T1156  
T1157  
T1158  
T1159  
T1160  
T1161  
T1162  
T1163  
T1164  
T1165  
T1166  
T1167  
T1168  
T1169  
T1170  
T1171  
T1172  
T1173  
T1174  
T1175  
T1176  
T1177  
T1178  
T1179  
T1180  
T1181  
T1182  
T1183  
T1184  
T1185  
T1186  
T1187  
T1188  
T1189  
T1190  
T1191  
T1192  
T1193  
T1194  
T1195  
T1196  
T1197  
T1198  
T1199  
T1200  
T1201  
T1202  
T1203  
T1204  
T1205  
T1206  
T1207  
T1208  
T1209  
T1210  
T1211  
T1212  
T1213  
T1214  
T1215  
T1216  
T1217  
T1218  
T1219  
T1220  
T1221  
T1222  
T1223  
T1224  
T1225  
T1226  
T1227  
T1228  
T1229  
T1230  
T1231  
T1232  
T1233  
T1234  
T1235  
T1236  
T1237  
T1238  
T1239  
T1240  
T1241  
T1242  
T1243  
T1244  
T1245  
T1246  
T1247  
T1248  
T1249  
T1250  
T1251  
T1252  
T1253  
T1254  
T1255  
T1256  
T1257  
T1258  
T1259  
T1260  
T1261  
T1262  
T1263  
T1264  
T1265  
T1266  
T1267  
T1268  
T1269  
T1270  
T1271  
T1272  
T1273  
T1274  
T1275  
T1276  
T1277  
T1278  
T1279  
T1280  
T1281  
T1282  
T1283  
T1284  
T1285  
T1286  
T1287  
T1288  
T1289  
T1290  
T1291  
T1292  
T1293  
T1294  
T1295  
T1296  
T1297  
T1298  
T1299  
T1300  
T1301  
T1302  
T1303  
T1304  
T1305  
T1306  
T1307  
T1308  
T1309  
T1310  
T1311  
T1312  
T1313  
T1314  
T1315  
T1316  
T1317  
T1318  
T1319  
T1320  
T1321  
T1322  
T1323  
T1324  
T1325  
T1326  
T1327  
T1328  
T1329  
T1330  
T1331  
T1332  
T1333  
T1334  
T1335  
T1336  
T1337  
T1338  
T1339  
T1340  
T1341  
T1342  
T1343  
T1344  
T1345  
T1346  
T1347  
T1348  
T1349  
T1350  
T1351  
T1352  
T1353  
T1354  
T1355  
T1356  
T1357  
T1358  
T1359  
T1360  
T1361  
T1362  
T1363  
T1364  
T1365  
T1366  
T1367  
T1368  
T1369  
T1370  
T1371  
T1372  
T1373  
T1374  
T1375  
T1376  
T1377  
T1378  
T1379  
T1380  
T1381  
T1382  
T1383  
T1384  
T1385  
T1386  
T1387  
T1388  
T1389  
T1390  
T1391  
T1392  
T1393  
T1394  
T1395  
T1396  
T1397  
T1398  
T1399  
T1400  
T1401  
T1402  
T1403  
T1404  
T1405  
T1406  
T1407  
T1408  
T1409  
T1410  
T1411  
T1412  
T1413  
T1414  
T1415  
T1416  
T1417  
T1418  
T1419  
T1420  
T1421  
T1422  
T1423  
T1424  
T1425  
T1426  
T1427  
T1428  
T1429  
T1430  
T1431  
T1432  
T1433  
T1434  
T1435  
T1436  
T1437  
T1438  
T1439  
T1440  
T1441  
T1442  
T1443  
T1444  
T1445  
T1446  
T1447  
T1448  
T1449  
T1450  
T1451  
T1452  
T1453  
T1454  
T1455  
T1456  
T1457  
T1458  
T1459  
T1460  
T1461  
T1462  
T1463  
T1464  
T1465  
T1466  
T1467  
T1468  
T1469  
T1470  
T1471  
T1472  
T1473  
T1474  
T1475  
T1476  
T1477  
T1478  
T1479  
T1480  
T1481  
T1482  
T1483  
T1484  
T1485  
T1486  
T1487  
T1488  
T1489  
T1490  
T1491  
T1492  
T1493  
T1494  
T1495  
T1496  
T1497  
T1498  
T1499  
T1500  
T1501  
T1502  
T1503  
T1504  
T1505  
T1506  
T1507  
T1508  
T1509  
T1510  
T1511  
T1512  
T1513  
T1514  
T1515  
T1516  
T1517  
T1518  
T1519  
T1520  
T1521  
T1522  
T1523  
T1524  
T1525  
T1526  
T1527  
T1528  
T1529  
T1530  
T1531  
T1532  
T1533  
T1534  
T1535  
T1536  
T1537  
T1538  
T1539  
T1540  
T1541  
T1542  
T1543  
T1544  
T1545  
T1546  
T1547  
T1548  
T1549  
T1550  
T1551  
T1552  
T1553  
T1554  
T1555  
T1556  
T1557  
T1558  
T1559  
T1560  
T1561  
T1562  
T1563  
T1564  
T1565  
T1566  
T1567  
T1568  
T1569  
T1570  
T1571  
T1572  
T1573  
T1574  
T1575  
T1576  
T1577  
T1578  
T1579  
T1580  
T1581  
T1582  
T1583  
T1584  
T1585  
T1586  
T1587  
T1588  
T1589  
T1590  
T1591  
T1592  
T1593  
T1594  
T1595  
T1596  
T1597  
T1598  
T1599  
T1600  
T1601  
T1602  
T1603  
T1604  
T1605  
T1606  
T1607  
T1608  
T1609  
T1610  
T1611  
T1612  
T1613  
T1614  
T1615  
T1616  
T1617  
T1618  
T1619  
T1620  
T1621  
T1622  
T1623  
T1624  
T1625  
T1626  
T1627  
T1628  
T1629  
T1630  
T1631  
T1632  
T1633  
T1634  
T1635  
T1636  
T1637  
T1638  
T1639  
T1640  
T1641  
T1642  
T1643  
T1644  
T1645  
T1646  
T1647  
T1648  
T1649  
T1650  
T1651  
T1652  
T1653  
T1654  
T1655  
T1656  
T1657  
T1658  
T1659  
T1660  
T1661  
T1662  
T1663  
T1664  
T1665  
T1666  
T1667  
T1668  
T1669  
T1670  
T1671  
T1672  
T1673  
T1674  
T1675  
T1676  
T1677  
T1678  
T1679  
T1680  
T1681  
T1682  
T1683  
T1684  
T1685  
T1686  
T1687  
T1688  
T1689  
T1690  
T1691  
T1692  
T1693  
T1694  
T1695  
T1696  
T1697  
T1698  
T1699  
T1700  
T1701  
T1702  
T1703  
T1704  
T1705  
T1706  
T1707  
T1708  
T1709  
T1710  
T1711  
T1712  
T1713  
T1714  
T1715  
T1716  
T1717  
T1718  
T1719  
T1720  
T1721  
T1722  
T1723  
T1724  
T1725  
T1726  
T1727  
T1728  
T1729  
T1730  
T1731  
T1732  
T1733  
T1734  
T1735  
T1736  
T1737  
T1738  
T1739  
T1740  
T1741  
T1742  
T1743  
T1744  
T1745  
T1746  
T1747  
T1748  
T1749  
T1750  
T1751  
T1752  
T1753  
T1754  
T1755  
T1756  
T1757  
T1758  
T1759  
T1760  
T1761  
T1762  
T1763  
T1764  
T1765  
T1766  
T1767  
T1768  
T1769  
T1770  
T1771  
T1772  
T1773  
T1774  
T1775  
T1776  
T1777  
T1778  
T1779  
T1780  
T1781  
T1782  
T1783  
T1784  
T1785  
T1786  
T1787  
T1788  
T1789  
T1790  
T1791  
T1792  
T1793  
T1794  
T1795  
T1796  
T1797  
T1798  
T1799  
T1800  
T1801  
T1802  
T1803  
T1804  
T1805  
T1806  
T1807  
T1808  
T1809  
T1810  
T1811  
T1812  
T1813  
T1814  
T1815  
T1816  
T1817  
T1818  
T1819  
T1820  
T1821  
T1822  
T1823  
T1824  
T1825  
T1826  
T1827  
T1828  
T1829  
T1830  
T1831  
T1832  
T1833  
T1834  
T1835  
T1836  
T1837  
T1838  
T1839  
T1840  
T1841  
T1842  
T1843  
T1844  
T1845  
T1846  
T1847  
T1848  
T1849  
T1850  
T1851  
T1852  
T1853  
T1854  
T1855  
T1856  
T1857  
T1858  
T1859  
T1860  
T1861  
T1862  
T1863  
T1864  
T1865  
T1866  
T1867  
T1868  
T1869  
T1870  
T1871  
T1872  
T1873  
T1874  
T1875  
T1876  
T1877  
T1878  
T1879  
T1880  
T1881  
T1882  
T1883  
T1884  
T1885  
T1886  
T1887  
T1888  
T1889  
T1890  
T1891  
T1892  
T1893  
T1894  
T1895  
T1896  
T1897  
T1898  
T1899  
T1900  
T1901  
T1902  
T1903  
T1904  
T1905  
T1906  
T1907  
T1908  
T1909  
T1910  
T1911  
T1912  
T1913  
T1914  
T1915  
T1916  
T1917  
T1918

S2  
P3  
  
P3  
P4  
  
P4  
P6  
  
P6  
P8  
  
P8  
P1  
  
P10  
P12  
  
P12  
P14  
  
P14  
P16  
  
P16

CYB  
END  
CALL  
EQU  
EQU  
CALL  
EQU  
EQU  
CALL  
EQU  
EQU  
CALL  
EQU  
EQU  
CALL  
EQU  
EQU  
CALL  
EQU  
EQU  
CALL  
EQU

42.

[illegible]

DU  
T2  
S3  
DO  
T3  
S4  
DO  
T4  
SF \*  
DO  
FX  
SD \*  
DU  
DX  
SF \*  
DO  
FX  
SD \*  
DU  
DX  
SF \*  
DU  
FX  
SD \*  
DO  
DX

XL	P28
XL	P4
XL	P52
XL	P64
XL	FX
XL	FX
XL	FX
XL	FX
XL	T66
XL	DX
XL	DX
XL	DX
XL	DX
XL	T68
XL	FX
XL	FX
XL	FX
XL	FX
XL	T79
XL	DX
XL	DX
XL	DX
XL	DX
XL	T2
XL	FX
XL	FX
XL	FX
XL	FX

P28	XL
P40	XL
P52	XL
P64	XL
FX	XL
FX	XL
FX	XL
FX	XL
FX	XL
T66	T67
DX	XL
DX	XL
DX	XL
DX	XL
DX	XL
T68	T69
FX	XL
FX	XL
FX	XL
FX	XL
FX	XL
T70	T71
DX	XL
DX	XL
DX	XL
DX	XL
T2	T3
FX	T4
FX	T5
FX	XL
FX	XL
FX	XL
FX	XL

P3	XL
P4 <sup>u</sup>	XL
P5 <sup>u</sup>	XL
P6 <sup>u</sup>	T67
DX	XL
DX	XL
DX	XL
DX	XL
T6 <sup>o</sup>	T69
FX	XL
FX	XL
FX	XL
FX	XL
T7 <sup>u</sup>	T1
DX	XL
DX	XL
DX	XL
DX	XL
T2	T3
FX	T15
FX	XL
FX	XL
FX	XL
T4	XL
DX	XL
DX	XL
DX	XL
DX	XL

[illegible]

P32	XL
P44	XL
P55	XL
P68	P69
FX	XL
FX	XL
FX	XL
FX	XL
T7	T1
DX	XL
DX	XL
DX	XL
DX	XL
T2	T3
FX	T15
FX	XL
FX	XL
FX	XL
T4	XL
DX	XL
DX	XL
DX	XL
DX	XL
DX	XL
FX	XL
FX	XL
FX	XL
T66	T67

[illegible]

P36  
P48  
P51  
P52  
TXX  
FX  
FX  
FX  
FX  
T4  
DX  
DX  
DX  
DX  
DX  
FX  
FX  
FX  
FX  
T55  
DX  
DX  
DX  
DX  
T58  
FX  
FX  
FX  
FX  
T79

Write tape.

P39	FCALL	SF*
P40	EQU	DU
P41	FCALL	FX*
P42	EQU	SD*
P43	FCALL	DU
P44	EQU	DX*
P45	FCALL	SF*
P46	EQU	DU
P47	FCALL	FX*
P48	EQU	SD*
P49	FCALL	DU
P50	EQU	DX*
P51	FCALL	SF*
P52	EQU	DU
P53	FCALL	FX*
P54	EQU	SD*
P55	FCALL	DU
P56	EQU	DX*
P57	FCALL	SF*
P58	EQU	DU

P53	CALL	DU
P61	EQU	FX
	EQU	SD*
	CALL	DO
P6	EQU	DX
P62	EQU	SF*
	CALL	DU
P62	EQU	FX
P64	EQU	SD*
	CALL	DU
P64	EQU	DX
P66	EQU	S05
	CALL	DO
P66	EQU	T06
P68	EQU	S68
	CALL	DO
P68	EQU	T68
P69	EQU	S69
	CALL	DU
	FIN	
	STOP	
EUF		

Appendix 2 OTRIM Listing

The program was kept on the CIMS tape at N.Y.U. in order to reduce the probability of transmission error. The corresponding control cards are shown above the listing of OTRIM and it is also shown where any desired changes to the program would be inserted. The reader should consult the CIMS User's Manual for explanation of how changes are made. The data cards shown are for a test case run (ITEST=1) including spy stations (ISPY=1) in the horizontal plane (NHOR=1) and with 5 Q matrices to be calculated (NNNQ=5). The numbers of small eigenvalue eigenvectors to be omitted are 108, 68, 28, 8, 0 respectively.

In order to demonstrate how an arbitrary misalignment may be introduced, we have shown, at the appropriate place in the listing, the changes required to run the 20th harmonic misalignment.

# OTRIM LISTING

```

EOF
G206002,T3400,CM337000,L4000. NAL REMOTE BINGHAM
REWIND(OUTPUT)
REQUEST CIMST.
CIMS3.
REQUEST,T312=TAPE3. READ SYNCH
REQUEST,T337=TAPE4. WRITE,READ T,M,Q.
REWIND(TAPE3)
REWIND(TAPE4)
MAP(PART)
RUNIG,,,TAPEZ,EROUT)
*CXIT.
EREDIT.
*FIN.
REMOTE OUTPUT,252.
EOR
$GET OTRIM L ← changes if any.
$LAST R
$END Z
EOR
108 1 1 1 0 0 0 0 0 5
EUF

```

Control  
Cards  
For  
OTRIM  
Stored  
on  
CIMS.  
Tape at  
NYU  
Data

```

PROGRAM OTRIM (INPUT=22,OUTPUT=22,TAPE3,TAPE4)
C OTRIM READS IN SYNCH OUTPUT SY FROM TAPE3, GENERATES S,G,T,EM(=M).
C T=S*G. B=T*H. EM=T(TRANPOSE)*T. GANGING MATRIX G=1 HERE.
C EIGEN DETERMINES E.VECTORS AND E.VALUES OF EM. Q MATRIX IS FOUND.
C HQ=B*Q ARE QUAD.POSITION CORRECTIONS,WHERE B ARE B.SENSOR READINGS.
C TAPE4 IS SCRATCH TAPE FOR T,M,AND AND Q/6 MATRICES
COMMON/F202/ AMP,HQ,W2,KAP
COMMON/F203/ INDEXX(223),TT(223,3),NQ(20)
DIMENSION EM(223,223),B(223,223),VALU(223),W1(223),W2(223)
DIMENSION AMP(223),AMPMX(4),IAMP(4),V(223,223),HQ(223),TEM(223)
DIMENSION GG(223,223),BS(223),H(223),BE(223),VVJM(223)
DIMENSION T(223,223),Q(223,223),SY(223,36),S(223,223)
DIMENSION G(223,223),KAP(223),R(223,223),BSP(223)
EQUIVALENCE (AMP,W1,BS),(S,T,EM,GG),(G,SY,R,B,V,Q),(HQ,TEM),(VALU,
1H),(W2,BE,BSP,VVJM)
LOIM=223
NH=222
NB=210
NBS=NB/6
NHS=NH/6
NGC=NH
NGR=NH
NSR=NB
NTR=NSR
NTC=NGC
NSC=NGR
READ 3010,ITEST,ISPY,NHOR,NVERT,KAPUTH,KAPUTV,NVCHEK,NHARM,NNNQ
3010 FORMAT (16I5)
IF(NHOR.NE.1.AND.NVERT.NE.1) 3051,3052
3051 PRINT 3050
3050 FORMAT (34HOTRIM WAS NOT ASKED TO DO ANYTHING)
CALL EXIT
3052 PRINT 3011,ITEST,ISPY,NHOR,NVERT,KAPUTH,KAPUTV,NVCHEK,NHARM,NNNQ

```

```

3011 FORMAT (19HINSTRUCTION CARD***,6HITEST=,I1,2X5HISPY=,I1,2X5HNNHOR=,
1I1,2X 6HNVERT=,I1,2X7HKAPUTH=,I3,2X7HKAPUTV=,I3,2X7HNVCKE=,I1,2X
26HNNHARM=,I1,2X5HNNNQ=,I1)
3020 CONTINUE
      REWIND 3
      REWIND 4
      IF(NHOR.EQ.1) GO TO 3030
      IF(NVERT.EQ.1) GO TO 3040
      CALL EXIT
3030 PRINT 3060
3060 FORMAT (1H1/,47H                                ORBIT ANALYSIS IN HORIZONTAL PLANE//)
      KAPUT=KAPUTH
      GO TO 3070
3040 PRINT 3080
3080 FORMAT (1H1/,45H                                ORBIT ANALYSIS IN VERTICAL PLANE//)
      KAPUT=KAPUTV
3070 CONTINUE
      DO 3090 J=1,36
      DO 3090 I=1,NB
      IF (NHOR.EQ.1) GO TO 3100
      READ (3,3120) MN,IPOS,KKK,EL,BETX5,SY(I,J),BETX7,BETY7
      GO TO 3090
3100 READ (3,3120) MN,IPOS,KKK,EL,SY(I,J),BETY5,BETX7,BETY7
3120 FORMAT (A5,2I3,5F14.8)
3090 READ (3,3120) MN,IPOS,KKK,EL,BETX5,BETY5,BETX7,BETY7
      READ (3,3120) EOF
      IF (EOF,3) 3130,3131
3131 PRINT 3140
3140 FORMAT (21HDO NOT FIND SYNCH EOF)
      CALL EXIT
3130 CONTINUE
6700 FORMAT (1X10(1XF9.5))
      NELAG=1
3078 FORMAT(1X2I2)
C EXPAND SY MATRIX AND SUBTRACT OUT BEAM SENSOR DISPLACEMENT TO GET
C DISP. OF BEAM RELATIVE TO B.SENSORS.
      S(1,1)=-1.
      DO 1204 I=2,NSR
1204  S(I,1)=0.
      DO 1207 I=1,NSR
      DO 1207 J=2,3
      IF (I.EQ.2) GO TO 1208
      S(I,J)=SY(I,(J-1))
      GO TO 1207
1208  S(I,J)=SY(I,(J-1))-0.5
1207 CONTINUE
      DO 1211 I=1,NSR
      DO 1211 J=4,35
      IF (I.EQ.(J-1)) GO TO 1210
      S(I,J)=SY(I,(J-1))
      GO TO 1211
1210  S(I,J)=SY(I,(J-1))-1.
1211 CONTINUE
      DO 1215 I=1,NSR
      DO 1215 J=36,37
      IF (I.EQ.35) GO TO 1214
      S(I,J)=SY(I,(J-1))
      GO TO 1215
1214  S(I,J)=SY(I,(J-1))-0.5
1215 CONTINUE
C GENERATE REMAINING 5/6 OF S MATRIX

```

```

      NSCS=NSC/6
      NSRS=NSR/6
      DO 1021 J=1,NSCS
      DO 1021 I=1,NSR
      DO 1021 N=1,5
      IF (I+N*NSRS-NSR) 1023,1023,1024
1023  S(I+N*NSRS,J+N*NSCS)=S(I,J)
      GO TO 1021
1024  S(I+N*NSRS-NSR,J+N*NSCS)=S(I,J)
1021  CONTINUE
1029  FORMAT (3(2F14.8,5X))
C CONSTRUCT GANGING MATRIX G.EXAMPLE TRIVIAL CASE G=1.
      DO 1050 J=1,NGC
      DO 1050 I=1,NGR
      IF (J.EQ.I) GO TO 1051
      G(I,J)=0
      GO TO 1050
1051  G(I,J)=1.
1050  CONTINUE
C CALCULATES T=S*G BY ROWS AND STORE IN T (EQUIV S) ROWS
      DO 1058 I=1,NSR
      DO 1057 J=1,NGC
      TEM(J)=0.
      DO 1057 K=1,NSC
1057  TEM(J)=TEM(J)+S(I,K)*G(K,J)
      DO 1059 L=1,NGC
1059  T(I,L)=TEM(L)
1058  CONTINUE
C CHECK ZERO SUM OF ELEMENTS OF EACH ROW OF T MATRIX
      DO 1085 I=1,NTR
      TEM(I)=0.
      DO 1085 J=1,NTC
1085  TEM(I)=TEM(I)+T(I,J)
      PRINT 6700,(TEM(I),I=1,NTR)
      NROW=0
      DO 1084 I=1,NTR
      IF (ABS(TEM(I)).GT.1.0E-6) NROW=1
1084  CONTINUE
      IF (NROW.EQ.1.AND.NHOR.EQ.1) PRINT 1083
1083  FORMAT (52H***ERROR SUM OF ELEMENTS OF T ROW GREATER 1.0E-6)
C REDUCE T MATRIX BY B.SENSORS THAT ARE KAPUT. R IS REDUCED T MATRIX
      IF (KAPUT.EQ.0) GO TO 3162
      READ 3160,(KAP(I),I=1,KAPUT)
3160  FORMAT (16I5)
      PRINT 3170
      PRINT 3160,(KAP(I),I=1,KAPUT)
3170  FORMAT (36HB.SENSORS CRAPPED OUT ARE AS FOLLOWS/)
3162  CONTINUE
      N=N-I
      DO 3180 I=1,NTR
      IF (KAPUT.EQ.0) GO TO 3200
      NNKAP=0
      DO 3190 L=1,KAPUT
      IF (KAP(L).EQ.I) NNKAP=1
3190  CONTINUE
      IF (NNKAP.EQ.1) GO TO 3180
3200  N=N+1
      DO 3210 J=1,NTC
3210  R(N,J)=T(I,J)
3180  CONTINUE
      NR=N

```



```

WRITE (4) (KAP(I),I=1,KAPUT)
DO 3191 I=1,NTR
3191 WRITE (4) (T(I,J),J=1,NTC)
END FILE 4
C CALCULATE M=EM=R*(TRANPOSE)*R
DO 1066 I=1,NTC
DO 1066 J=1,NTC
EM(I,J)=0.
DO 1066 K=1,NR
1066 EM(I,J)=EM(I,J)+R(K,I)*R(K,J)
DO 6210 I=1,NTC
6210 WRITE (4) (EM(I,J),J=1,NTC)
END FILE 4
C ONLY NR OF THE NTC E.VALUES WILL BE NON ZERO
CALL TIME (9HSTART EIG)
CALL EIGEN(EM,B,NTC,VALU,NR,SRNORM,LDIM)
CALL TIME (7HEND EIG)
PRINT 6070,SRNORM
6070 FORMAT (1X,7HSRNORM=E30.14)
C MOVE E.VECTORS FROM COLUMNS OF EM TO COLUMNS OF V
DO 6230 I=1,NTC
DO 6230 J=1,NR
6230 V(I,J)=EM(I,J)
C READ EM BACK IN FROM TAPE4 .STEP THROUGH T FIRST
REWIND 4
READ (4) (KAP(I),I=1,KAPUT)
DO 6220 I=1,NTR
6220 READ (4) EM(I,1)
READ (4) EOF
IF (EOF,4) 6230,6240
6240 PRINT 6250
6250 FORMAT (10HMISS T EOF)
CALL EXIT
6230 CONTINUE
DO 6032 I=1,NTC
6032 READ (4) (EM(I,J),J=1,NTC)
READ (4) EOF
IF (EOF,4) 6033,6006
6006 PRINT 6007
6007 FORMAT (1X20HCANNOT FIND EOF ON M)
CALL EXIT
6033 CONTINUE
IF (NVCHK.NE.1) GO TO 6300
CALL VCHK(LDIM,V,VALU,W1,W2,NTC,NR,EM)
6300 CONTINUE
IF (NHARM.NE.1) GO TO 6400
C FOURIER ANALYSIS OF G*V. RELOAD GANGING MATRIX G INTO GG.(G=1)
CALL TIME (9HSTART HAR)
DO 6310 I=1,NGR
DO 6310 J=1,NGC
IF (I.EQ.J) GO TO 6320
GG(I,J)=0.
GO TO 6310
6320 GG(I,J)=1.
6310 CONTINUE
DO 6330 K=1,NTC
DO 6340 I=1,NGR
TEM(I)=0.
DO 6340 J=1,NGC
6340 TEM(I)=TEM(I)+GG(I,J)*V(J,K)
CALL HAR(TEM,W2,NH)

```

```

NGR2=NGR/2
NGR1=NGR/2+1
AMP(1)=W2(1)
AMP(NGR1)=W2(NGR1)
DO 6350 L=2,NGR2
M=NGR2+L
6350 AMP(L)=SQRT((W2(L))**2+(W2(M))**2)
DO 6081 MM=1,4
AMPMX(MM)=AMP(L)
IAMP(MM)=0
DO 6080 L=2,NGR1
IF(AMP(L).LT.AMPMX(MM)) GO TO 6080
AMPMX(MM)=AMP(L)
IAMP(MM)=L-1
6080 CONTINUE
IM=IAMP(MM)+1
AMP(IM)=0.
6081 CONTINUE
PRINT 6082,(AMPMX(I),I=1,4),(IAMP(I),I=1,4),VALU(K),K
6082 FORMAT (1X4(1XE12.5),15X,4(2XI3),5XE12.6,5XI3)
6330 CONTINUE
CALL TIME (7HEND HAR)
6400 CONTINUE
C GENERATE Q MATRIX.NQS,NQL ARE SUM LIMITS AT SMALL,LARGE E.VALUES RESP.
C E.VALUES =J ARE EXCLUDED (NIC-NR).Q/6 IS GENERATED,SYMMETRY GIVES REM.
C READ IN T MATRIX IN PLACE OF GG
REWIND 4
READ (4) (KAP(I),I=1,KAPUT)
DO 6087 I=1,NTR
6087 READ (4) (T(I,J),J=1,NTC)
READ (4) EOF
IF(EOF,4) 6088,6089
6089 NFLAG=8
PRINT 3078,NFLAG
CALL EXIT
6088 CONTINUE
C STORE NQS OF OPERATING B.SENSORS IN INDEXX.
N=0
DO 6095 I=1,NTR
IF(KAPUT.EQ.0) GO TO 6096
NNKAP=0
DO 6097 L=1,KAPUT
IF(KAP(L).EQ.I) NNKAP=1
6097 CONTINUE
IF(NNKAP.EQ.1) GO TO 6095
6096 N=N+1
INDEXX(N)=I
6095 CONTINUE
CALL TIME (7HSTART Q)
C NQ(I) MUST RUN FROM LARGEST TO SMALLEST NUMBER .Q/6 WRITTEN OVER T.
READ 3160,(NQ(I),I=1,NNNQ)
PRINT 6410,(NQ(I),I=1,NNNQ)
6410 FORMAT (76HQ MATRICES OBTAINED FOR DELETION OF FOLLOWING NUMBERS 0
IF SMALL E.VECTORS****/,1X16I5)
REWIND 4
DO 6500 I=1,NNNQ
6500 NQ(NNQ+2-I)=NR-NQ(NNQ+1-I)
NQ(1)=0
3077 FORMAT (4HNTC=,I3,5X3HNR=,I3,5X3HNB=,I3,5X5HNNNQ=,I3)
DO 6094 M=1,NTC
DO 6510 IJ=1,NB

```

```

6510 TEM(I,J)=0.
DO 6092 J=1,NTC
6092 VVJM(J)=0.
DO 6094 I=1,NNNQ
NQS=NQ(I,I+1)
NQL=NQ(I,I)+1
DO 6093 J=1,NTC
DO 6093 N=NQL,NQS
6093 VVJM(J)=VVJM(J)+V(J,N)*V(M,N)/VALU(N)
DO 6090 I=1,NR
I1=INDEXX(I)
SUM=0.
DO 6091 J=1,NTC
6091 SUM=SUM-T(I1,I,J)*VVJM(J)
6090 TEM(I)=SUM
WRITE (4) (TEM(I),I=1,NR)
6094 CONTINUE
PRINT 3077,NTC,NR,NB,NNNQ
END FILE 4
CALL TIME(5HEND Q)
C READ Q BACK FROM TAPE4
REWIND 4
DO 220 KK=1,NNNQ
PRINT 3078,KK
IF (KK.EQ.1) GO TO 520
KK=KK-1
DO 530 KKK=1,KK1
530 READ (4) (TEM(M),M=1,NR)
520 CONTINUE
DO 540 M=1,NTC
READ (4) (Q(I,M),I=1,NR)
IF (M.EQ.NTC) GO TO 540
NNNQ=NNNQ-1
DO 510 LL=1,NNNQ1
510 READ (4) (TEM(I),I=1,NR)
540 CONTINUE
711 CONTINUE
IF (KK.NE.1) GO TO 680
IF (TEST.EQ.1) GO TO 700
IF (IN B.SENSOR READINGS BS(I) AND OBTAIN CORRECTIONS OF QUADS HQ(I))
C READ 610, (TEM(I),I=1,NB)
610 FORMAT (8F10.4)
IF (KAPUT.EQ.0) GO TO 680
DO 611 I=1,NR
I1=INDEX(I)
611 BS(I)=TEM(I1)
GO TO 680
720 CONTINUE
C FOR TEST ASSUME FIRST QUAD AT LONG STRAIGHT DISPLACED =+1 20th HARMONIC
C THEN BS(I)=T(I,2)
H(1)=0.
H(2)=1.
DO 660 I=3,NH
FOR 20th HARMONIC
REPLACE AS SHOWN
660 H(I)=0.
DO 662 I=1,NB
662 TEM(I)=T(I,2)
DO 640 I=1,NR
I1=INDEXX(I)
640 BS(I)=TEM(I1)
680 CONTINUE
IF (KK.EQ.1.AND.NHOR.EQ.1) GO TO 820
DO 662 J=1, NH
TEM(I)=0.
PRINT 6700, (H(I),I=1,NH)
DO 662 I=1, NB
H(I)=0.
DO 661 I=16, NH
H(I)=0.
DO 659 I=1,5
H(I)=0.
659
660
661

```

662 TEM(I)=TEM(I)+T(I,J)\*H(J)  
 PRINT 6700, (TEM(I), I=1,NB)  
 DO 640 I=1,NR  
 640 BI=INDEX(I)  
 BS(I)=TEM(LI)

IF(KK.EQ.1.AND.NVERT.EQ.1) GO TO 833  
 GO TO 829  
 820 PRINT 822,KAPUT  
 GO TO 829  
 830 PRINT 824,KAPUT  
 822 FORMAT (43HORIZONTAL PLANE,NUMBER OF B.SENSORS KAPUT=,I3//)  
 824 FORMAT (41HVERTICAL PLANE,NUMBER OF B.SENSORS KAPUT=,I3//)  
 829 CONTINUE

DO 810 I=1,NH  
 HQ(I)=0.  
 DO 810 J=1,NR  
 810 HQ(I)=HQ(I)+BS(J)\*Q(J,I)  
 N=NR-NQ(KK+1)

PRINT 460,N,NR  
 460 FORMAT (1X13,6HOF THE,I3,59HNONZERO E.VECTORS OMITTED. RECOMMENDED  
 1 POSITION CORRECTIONS)  
 PRINT 500,(HQ(I),I=1,NH)  
 500 FORMAT (1X10(F10.7))

HQTOT=0.  
 DO 200 I=1,NH  
 200 HQIDI=HQIDI+ABS(HQ(I))

PRINT 201,HQTOT  
 201 FORMAT (29HTOTAL MAGNET DISP. HQTOT=,E10.3)  
 IF(ITEST.NE.1) GO TO 220

C OBTAIN RESIDUAL BEAM ERROR BE(I) AFTER QUAD.POSITIONS CORRECTED  
 DO 90 I=1,NR  
 BE(I)=0.

DO 90 J=1,NH  
 90 BE(I)=BE(I)+I(J,J)\*(H(I,J)+HQ(J))

C DETERMINE MAX,RMS,RMSMAX,DISPLACEMENTS OF EQUILIB ORBIT BEFORE AND AFT  
 C ER CORRECTION.

IF(KK.NE.1) GO TO 850  
 CALL NUMBER (BS,BSMAX,BSRMS,BSMRMS,NR)

850 CONTINUE  
 CALL NUMBER (BE,BEMAX,BERMS,BEMRMS,NR)

PRINT 440  
 PRINT 441,(BE(I),I=1,NB)

440 FORMAT (49HBEAM WRT DISP.STRUCTURE AFTER CORRECTIONS APPLIED//)  
 441 FORMAT (1X10(1XE9.2))

235 FORMAT (15HVECTORS OMITTED,2X,8HBMAXIMUM,12X,12HBROOT MEAN S ,8X,1  
 16HBMAX ROOT MEAN S,4X,14HTOTAL MAG DISP)

PRINT 240,BSMAX,BSRMS,BSMRMS  
 PRINT 245,N,BEMAX,BERMS,BEMRMS,HQTOT

240 FORMAT (4X,3(10XE10.3),14X17HINITIAL CONDITION)  
 245 FORMAT (1X13,4(10XE10.3)///)

REWIND 4  
 IF (ITEST.EQ.1.AND.ISPY.EQ.1) GO TO 860  
 GO TO 220

860 CONTINUE  
 C READ IN SYNC RESULTS FOR SPY STATIONS

REWIND 3  
 DO 6590 J=2,37

DO 6590 I=1,NB  
 READ (3,3120) MN,IPOS,KKK,EL,BETX5,BETY5,BETX7,BETY7  
 IF (NHOR.EQ.1) GO TO 6600  
 READ (3,3120) MN,IPOS,KKK,EL,BEIX5,SY(I,J),BEIX7,BEIX7  
 GO TO 6590

6600 READ (3,3120) MN,IPOS,KKK,EL,SY(I,J),BETY5,BETX7,BETY7  
 6590 CONTINUE

C EXPAND SPY SY MATRIX FOR HIL.....222) CONVERT TO RELATIVE DISPL.

```

C NO. SPY STATIONS =NB ,NO.ACCEL.DISP. STILL NH.
DO 6610 I=1,NB
6610 SY(I,1)=0.
SY(I,2)=SY(I,2)-1.
DO 6611 J=4,NHS
I=J-2
6611 SY(I,J)=SY(I,J)-1.
DO 6620 J=1,NHS
DO 6620 I=1,NB
DO 6620 NN=1,5
IF(I+NN*NBS-NB) 6630,6630,6640
6630 SY(I+NN*NBS,J+NN*NHS)=SY(I,J)
GO TO 6620
6640 SY(I+NN*NBS-NB,J+NN*NHS)=SY(I,J)
6620 CONTINUE
DO 6650 I=1,NB
BSP(I)=0.
DO 6650 J=1,NH
6650 BSP(I)=BSP(I)+SY(I,J)*(H(J)+HQ(J))
PRINT 6660
6660 FORMAT (76HRELATIVE POSITION OF BEAM AT SPY STATIONS AFTER CORRECT
ION OF QUAD POSITIONS/)
PRINT 441,(BSP(I),I=1,NB)
220 CONTINUE
IF(NHOR.NE.1) GO TO 870
NHOR=0
IF(INVERT.EQ.1) GO TO 3020
870 CONTINUE
RETURN
END
SUBROUTINE NUMBER(CI,CMAX,CRMS,CMRMS,NB)
DIMENSION CI(223)
COMMON/F203/ INDEXX(223),C(224),VC(224)
DO 50 I=1,NB
50 C(I)=CI(I)
IMAX=1
CMAX=ABS(C(1))
DO 30 I=2,NB
IF (ABS(C(I)).GT.CMAX) GO TO 20
GO TO 30
20 CMAX=ABS(C(I))
IMAX=I
30 CONTINUE
CMS=0.
DO 40 I=1,NB
40 CMS=CMS+C(I)**2/NB
CRMS=SQRT(CMS)
C(NB+1)=C(1)
C(NB+2)=C(2)
II=0
DO 60 I=1,NB
IF(ABS(C(I+2)).LE.ABS(C(I+1)).AND.ABS(C(I+1)).GT.ABS(C(I))) GO TO
161
GO TO 60
61 II=II+1
VC(II)=ABS(C(I+1))
60 CONTINUE
140 FORMAT (1X5(10XE9.2))
CMMS=0.
DO 100 I=1,II
100 CMMS=CMMS+VC(I)**2/II

```

```

      CMRMS=SQRT(CMMS)
      RETURN
    END
    SUBROUTINE TIME(WORD)
    CALL SECOND(I)
    PRINT 10,T,WORD
10  FORMAT(4H0***F10.4,5X,A10)
    RETURN
    END
    SUBROUTINE EIGEN (A,B,NSUB,VALU,MSUB,SRNORM,NMAX)
    EIGENVALUES AND EIGENVECTORS OF A REAL SYMMETRIC MATRIX
C  SUB EIGEN RETURNS VECTORS IN COLUMNS OF EM.EIGENVALUES RETURN IN VALU.
C  B IS SPACE FOR STORAGE
    DIMENSION A(NMAX,NSUB), B(NMAX,NSUB), VALU(MSUB)
    DIMENSION
1    DIAG(223), SUPERD(223), WVEC(223), PVEC(223),
2    QVEC(223), VALL(223), Q(223), U(223),
    INDEX(223), FACTOR(223), V(223), T(223,3)
    COMMON/F202/ DIAG,SUPERD,WVEC,PVEC
    COMMON/F203/ INDEX,T
    EQUIVALENCE (WVEC,VALL, FACTOR,U), (PVEC,QVEC,Q,V), (I1,T1),
1    (I2,I2,ITER), (TEMP, T0), (SUM,MATCH), (I,P),
2    (DIV,SCALAR,TAU), (ANORM2,ANORM,SUPERD(223)),
3    (VTEMP,VNORM2,VNORM,INDEX(223))
    DATA (E1=2.0E-14)
C  HOUSEHOLDER SIMILARITY TRANSFORMATION TO CO-DIAGONAL FORM
    N=NSUB
    M=MSUB
    IF (M) 50, 50, 10
C  GENERATE IDENTITY MATRIX
10  DO 40 I=2,N
    DO 40 J=2,N
    B(J,I)=0.0
    IF ((I-J) 40, 25
25  B(J,I)=1.0
40  CONTINUE
50  DO 200 I=1,N
C  REDUCE COLUMN OF MATRIX
    I1=I+1
    I2=I1+1
    IF(I2.GT.N) GO TO 160
    SUM=0.0
    DO 70 J=I2,N
70  SUM=SUM+A(J,I)**2
    IF (SUM) 75,160,75
75  J=I1
    TEMP=A(J,I)
    SUM=SQRT(SUM+ TEMP **2)
    A(J,I)=-SIGNF(SUM, TEMP )
    WVEC(J)=SQRT( 1.0+ABSE( TEMP )/SUM)
    DIV=SIGNF( WVEC(J)*SUM, TEMP )
    DO 85 J=I2,N
85  WVEC(J)=A(J,I)/DIV
    SCALAR=0.0
    DO 95 J=I1,N
    PVEC(J)=0.0
    DO 90 K=I1,N
90  PVEC(J)=PVEC(J)+A(K,J)*WVEC(K)
    SCALAR=SCALAR+PVEC(J)*WVEC(J)
95  CONTINUE
    SCALAR=SCALAR/2.0
    DO 120 J=I1,N

```

```

      QVEC(J)=PVEC(J)-SCALAR*WVEC(J)
      DO 120 K=I1,J
      A(K,J)=A(K,J)-(WVEC(K)*QVEC(J)+WVEC(J)*QVEC(K))
      A(J,K)=A(K,J)
120  CONTINUE
      IF (M) 160, 160, 130
C     SAVE ROTATION FOR LATER APPLICATION TO CO-DIAGONAL VECTORS
130  DO 150 K=2,N
      TEMP=0.0
      DO 140 J=I1,N
140  TEMP=TEMP+WVEC(J)*B(J,K)
      DO 150 J=I1,N
      B(J,K)=B(J,K)-WVEC(J)*TEMP
150  CONTINUE
C     MOVE CO-DIAGONAL FORM ELEMENTS FOR ITERATIVE PROCEDURE
160  J=I
      DIAG(I)=A(J,I)
      SUPERD(I)=A(J+1,I)
200  CONTINUE
C     GIVENS EIGENVALUE ITERATION FROM STURM CHAIN OF CO-DIAGONAL MINORS
      N=XABSF(N)
      M=XABSF(M)
C     CALCULATE NORM OF MATRIX AND INITIALIZE EIGENVALUE BOUNDS
      ANORM2=DIAG(1)**2
      DO 230 L=2,N
      Q(L-1)=SUPERD(L-1)**2
      ANORM2=DIAG(L)**2+Q(L-1)+Q(L-1)+ANORM2
230  CONTINUE
      ANORM=SQRT(ANORM2)
      DO 240 L=1,M
      VALU(L)=ANORM
      VALL(L)=-ANORM
240  CONTINUE
      EPS1=ANORM*E1
      IF (EPS1) 250, 1000
250  DO 570 L=1,M
C     CHOOSE NEW TRIAL VALUE WHILE TESTING BOUNDS FOR CONVERGENCE
260  TAU=(VALU(L)+VALL(L))/2.0
      IF (2.0*(TAU-VALL(L))-EPS1) 570, 570, 270
C     DETERMINE SIGNS OF PRINCIPAL MINORS
270  MATCH=0
      T2=0.0
      T1=1.0
      DO 450 L1=1,N
      P=DIAG(L1)-TAU
      IF (T2) 330, 300
300  T1=SIGNF(1.0,T1)
330  IF (T1) 400, 370
370  T0=-SIGNF(1.0,T2)
      T2=0.0
      IF (Q(L1-1)) 410, 300
400  T0=P-Q(L1-1)*T2/T1
      T2=1.0
C     COUNT AGREEMENTS IN SIGN (ZERO CONSIDERED POSITIVE)
410  IF (T0) 440, 420, 430
420  T2=T1
      IF (T2) 440, 430, 430
430  MATCH=MATCH+1
440  T1=T0
450  CONTINUE
C     ESTABLISH TIGHTER BOUNDS ON EIGENVALUES

```

```

      DO 530 L1=L,M
      IF (L1-MATCH) 500, 500, 470
470  IF (VALU(L1)-TAU) 260, 260, 480
480  VALU(L1)=TAU
      GO TO 530
500  VALL(L1)=TAU
530  CONTINUE
      GO TO 260
570  CONTINUE
C    EIGENVECTORS OF CO-DIAGONAL SYMMETRIC MATRIX--INVERSE ITERATION
      M=MSUB
      DO 970 I=1,M
C    CHECK FOR REPEATED VALUE
      IF (I.EQ.1) GO TO 725
      IF (VALU(I-1)-VALU(I)-(1.0E4)*EPS1) 730,725,725
725  II=-1
730  II=II+1
C    TRIANGULARIZE CO-DIAGONAL FORM AFTER EIGENVALUE SUBTRACTION
      DO 760 L=1,N
      V(L)=EPS1
      T(L,2)=DIAG(L)-VALU(I)
      IF (L=N) 740, 735
735  T(L,3)=0.0
      GO TO 760
740  T(L,3)=SUPERD(L)
      IF (T(L,3)) 750, 745
745  T(L,3)=EPS1
750  T(L+1,1)=T(L,3)
760  CONTINUE
      DO 820 J=1,N
      T(J,1)=T(J,2)
      T(J,2)=T(J,3)
      T(J,3)=0.0
      VTEMP=ABS(T(J,1))
      IF (J=N) 785, 770
770  IF (VTEMP) 820, 780
780  T(J,1)=EPS1
      GO TO 820
785  INDEX(J)=0
      IF (ABS(T(J+1,1))-VTEMP) 810, 810, 790
790  INDEX(J)=1
      DO 800 K=1,3
      VTEMP=T(J,K)
      T(J,K)=T(J+1,K)
      T(J+1,K)=VTEMP
800  CONTINUE
810  VTEMP =T(J+1,1)/T(J,1)
      FACTOR(J)=VTEMP
      T(J+1,2)=T(J+1,2)- VTEMP *T(J,2)
      T(J+1,3)=T(J+1,3)- VTEMP *T(J,3)
820  CONTINUE
      ITER=1
      IF (II) 920, 860
C    BACK SUBSTITUTE TO OBTAIN EIGENVECTOR
860  DO 870 L1=1,N
      L=N+1-L1
      V(L)=(V(L)-T(L,2)*V(L+1)-T(L,3)*V(L+2))/T(L,1)
870  CONTINUE
      GO TO (875,920), ITER
C    PERFORM SECOND ITERATION
875  ITER=2

```



```

880 DO 910 L=2,N
    IF (INDEX(L-1))890,900
890 VTEMP=V(L-1)
    V(L-1)=V(L)
    V(L)=VTEMP
900 V(L)=V(L)-FACTOR(L-1)*V(L-1)
910 CONTINUE
    GO TO 860
C   ORTHOGONALIZE VECTOR TO OTHERS ASSOCIATED WITH REPEATED VALUE
920 IF(II.EQ.0) GO TO 945
    DO 940 LI=1,II
        K=I-LI
        VTEMP=0.0
        DO 930 J=1,N
            VTEMP=VTEMP+A(J,K)*V(J)
        DO 940 J=1,N
            V(J)=V(J)-A(J,K)*VTEMP
        GO TO (880,945), ITER
C   NORMALIZE VECTOR
945 VNORM2=0.0
    DO 950 L=1,N
        VNORM2=VNORM2+V(L)**2
    VNORM=SQRTF(VNORM2)
    DO 960 J=1,N
        A(J,I)=V(J)/VNORM
960 CONTINUE
C   ROTATION OF CO-DIAGONAL VECTORS INTO MATRIX EIGENVECTORS
    N=NSUB
    DO 990 I=1,M
        DO 980 K=2,N
            U(K)=0.0
        DO 980 J=2,N
            U(K)=U(K)+B(J,K)*A(J,I)
980 DO 990 J=2,N
        A(J,I)=U(J)
1000 SRNORM=ANORM
    RETURN
END
SUBROUTINE VCHEK(IRD,V,R,TEM,CC,NI,III,A)
    DIMENSION V(223,223),A(223,223),R(223),CC(223),TEM(223)
    M=NI
    DO 270 K=1,III
        DO 271 I=1,M
            SUM=0.0
            DO 272 J=1,M
                SUM=SUM+A(I,J)*V(J,K)
            CONTINUE
            TEM(I)=SUM
        CONTINUE
        DO 273 I=1,III
            SUM=0.0
            DO 274 J=1,M
                SUM=SUM+TEM(J)*V(J,I)
            CONTINUE
            CC(I)=SUM
        CONTINUE
        IL=K-1
        IF(K.EQ.1) IL=2
        DO 700 II=1,III
            IF(II.EQ.K) GO TO 700
            IF(ABS(CC(II)).GT. CC(IL)) IL=II

```

```

700 CONTINUE
XIL=.0000000001
IF(R(K).GT.0) XIL=XIL+R(K)*.00000002
IF(ABS(CC(IL)).LT.XIL.AND.ABS(R(K)-CC(K)).LT.XIL) GO TO 709
PRINT 705 , K,R(K),CC(K),IL,XIL,CC(IL)
705 FORMAT(1H0 I3,2E25.14,I7,2E25.14,7H ***** )
GO TO 712
709 PRINT 710 , K,R(K),CC(K),IL,XIL,CC(IL)
710 FORMAT(1H0 I3,2E25.14,I7,2E25.14)
712 CONTINUE
270 CONTINUE
280 RETURN
END
SUBROUTINE HAR(V,W,MIN)
COMMON/F203/ TBL(223),A(112),B(112),C(112),D(112),NC
DOUBLE PRECISION TBL
DIMENSION V(1),W(1)
CALL HASTBL(MIN)
N=NC/2
IMAX=N+1
A(1)=V(1)
B(1)=0.0
DO 5 I=2,IMAX
L=NC+2-I
A(I)=V(I)+V(L)
B(I)=V(I)-V(L)
5 CONTINUE
A(IMAX)=V(IMAX)
CALL HARSUM
F=1.0/FLOAT(N)
DO 9 I=1,IMAX
W(I)=C(I)*F
IF (I.GE. IMAX) GO TO 9
8 CONTINUE
K=N+I
W(K)=D(I)*F
9 CONTINUE
W(1)=0.5*W(1)
W(IMAX)=0.5*W(IMAX)
RETURN
END
SUBROUTINE HASTBL(MIN)
COMMON/F203/ TBL(223),A(112),B(112),C(112),D(112),NC
DOUBLE PRECISION TBL
DOUBLE PRECISION PI,FNC,SAVE,FI,DCI,DST,DB
EQUIVALENCE (PI,PO)
DIMENSION PO(2)
DATA PO / 1721 6220 7732 5042 0550 B, 1641 6043 2304 6146 1213 B /
IF (MIN.EQ. NC) RETURN
FNC=0.000
FI=0.000
NC=MIN
FNC=FLOAT(NC)
DB=PI/FNC
IF (MOD(NC,2) .NE. 0) GO TO 99
IF (NC.LE.222) GO TO 2
99 CONTINUE
PRINT 1000, NC
1000 FORMAT ( 14H0 ILLEGAL N. ,I20 )
STOP
2 CONTINUE

```

```

N=NC/2
NQ2=N/2
TBL(1)=1.0D0
TBL(N+1)=0.0D0
TBL(NC+1)=-1.0D0
IEO=2-MOD(N,2)
DO 9 I=IEO,NQ2,IEO
FI=FLOAT(I)
SAVE=FI*DB
DCT=DCOS(SAVE)
DST=DSIN(SAVE)
TBL(I+1)=DCT
K=N-I
TBL(K+1)=DST
K=K+N
TBL(K+1)=-DCT
K=N+I
TBL(K+1)=-DST
9 CONTINUE
RETURN
END
SUBROUTINE HARSUM
COMMON/F203/ TBL(223),A(112),B(112),C(112),D(112),NC
DOUBLE PRECISION TBL
DOUBLE PRECISION AJ,BJ,CI,DI
MR(K)=MIN0((MOD(K,NX4)),NX4-(MOD(K,NX4)))
AJ=0.0D0
BJ=0.0D0
NX3=(NC*3)/2
NX4=NC*2
IMAX=NC/2+1
IJA=0
DO 9 I=1,IMAX
CI=0.0D0
DI=0.0D0
IJ=0
DO 8 J=1,IMAX
IJC=MR(IJ)
IJS=MR(IJ+NX3)
AJ=DBLE(A(J))
BJ=DBLE(B(J))
CI=CI+AJ*TBL(IJC+1)
DI=DI+BJ*TBL(IJS+1)
IJ=IJ+IJA
8 CONTINUE
C(I)=SNGL(CI)
D(I)=SNGL(DI)
IJA=IJA+2
9 CONTINUE
RETURN
END
BLOCK DATA
COMMON/F203/ TBL(223),A(112),B(112),C(112),D(112),NC
DOUBLE PRECISION TBL
DATA NC / 0 /
END
EOF

```

### Appendix 3 Harmonic Response of Main Ring

The harmonic response of the Main Ring is obtained by the computer program HRESPON which is listed below. Starting from the SYNCH output tape HRESPON sets up the T matrix of Eqn. (2) by the same method used in OTRIM with the ganging matrix  $G=1$ . Then a set of beam element displacements is generated by

$$H(K) = \sin (0.001 \times I \times EE(K) + \phi(J)) \quad (A1)$$

with  $\phi(J) = 2\pi (J-1) / NFI \quad (A2)$

where  $I$  = harmonic number

$EL(K)$  = orbital distance to center of Kth beam  
element (metre)

$\phi(J)$  is the phase difference which may take  $NFI$   
equally spaced values on the interval  $0 -$   
 $2\pi$  as the index  $J$  is incremented.

For each harmonic  $I$ , HRESPON hunts on  $J$  to determine the phase  $\phi(J)$  at which the maximum closed orbit deviation occurs. It also hunts on  $J$  to determine the phase at which the r.m.s. orbit deviation is a maximum. The output lists, for each harmonic,

$I$  = harmonic number

$NM$  = beam element where max. orbit deviation occurred

$BMMAX$  = max. orbit deviation

$PHM$  = phase  $\phi(J)$  for max. orbit deviation

$NRM$  = beam element where max. orbit deviation occurred  
for max. r.m.s. orbit deviation case.

BRMMAX = max. r.m.s. orbit deviation

PHRM = phase  $\phi(J)$  for max. r.m.s. orbit deviation

The program requires only 1 data card (16I5) which specifies the variables -

NHOR = 0 skip horizontal plane

= 1 run horizontal plane

NVERT = 0 skip vertical plane

= 1 run vertical plane

NHAR - highest harmonic to be run (150 in listing below)

NFI - phase increments on interval  $0 - 2\pi$  (10 in listing below)

In Figure 15 and Figure 16 we have plotted the Main Ring harmonic response for the horizontal and vertical planes. The curves have the same general form as that obtained by Laslett<sup>8</sup>. The positions of the maxima are in good agreement with the expected positions as given by  $|6m \pm v_0|$  where  $m$  is an integer and  $v_0 = 20$  is the integer closest to the  $v$  value. The harmonic response of possible surveying schemes for the Main Ring are typically peaked towards low harmonics<sup>8</sup> due to short range correlations. Thus, although Figures 15 and 16 have large peaks at high harmonics, we would expect that the residual harmonics will peak at the integer (20) nearest the  $v$  value when the harmonic response of the survey system is included.



```

670-  FORMAT (1X,F9.5))
671-  FORMAT (1X,F1.3))
C  EXPAND SY MATRIX AND SUBTRACT OUT BEAM SENSOR DISPLACEMENT TO GET DISP
C  OF BEAM RELATIVE TO B.SENSORS.
      S(1,1)=1.
      DO 1204 I=2,NSR
        S(1,I)=0.
      DO 1207 I=1,NSR
        DO 1211 J=2,3
          IF(I.EQ.2) GO TO 1213
          S(I,J)=SY(I,(J-1))
          GO TO 1211
        S(I,J)=SY(I,(J-1))-1.5
      CONTINUE
      DO 1211 I=1,NSR
        DO 1211 J=4,35
          IF(I.EQ.(J-1))GO TO 1213
          S(I,J)=SY(I,(J-1))
          GO TO 1211
        S(I,J)=SY(I,(J-1))-1.
      CONTINUE
      DO 1215 I=1,NSR
        DO 1215 J=36,37
          IF(I.EQ.35) GO TO 1214
          S(I,J)=SY(I,(J-1))
          GO TO 1215
        S(I,J)=SY(I,(J-1))-0.5
      CONTINUE
C  GENERATE REMAINING 5/6 OF S MATRIX
      NSCS=NSC/6
      NSRS=NSR/6
      DO 1221 J=1,NSCS
        DO 1221 I=1,NSR
          DO 1221 N=1,5
            IF(I+N*NSRS-NSR) 1223,1223,1224
            S(I+N*NSRS,J+N*NSCS)=S(I,J)
            GO TO 1221
          S(I+N*NSRS-J+N*NSCS)=S(I,J)
          CONTINUE
          PRINT 1229,S(176,2),S(1,39),S(1,2),S(36,39),S(141,2),S(1,75)
          FORMAT (3(2F14.8,5X))
C  CHECK ZERO SUM OF ELEMENTS OF EACH ROW OF S MATRIX
      DO 1285 I=1,NTR
        TEM(I)=0.
        DO 1285 J=1,NTC
          TEM(I)=TEM(I)+S(I,J)
        PRINT 570,(TEM(I),I=1,NTR)
      NROW=7
      DO 1284 I=1,NTR
        IF(ABS(TEM(I)).GT.1.E-6)NROW=1
      CONTINUE
      IF(NROW.EQ.1) PRINT 1283
C  FORMAT (52H**ERROR.
C  CALCULATE NH H DIST.AROUND RING FROM NB B.SENSOR DISTANCES,EL(I).EL(I)
      =0.
      EL(37)=EL(35)+2.74353
      EL(36)=EL(35)-2.384945
      EL(35)=EL(34)-1.62635
      DO 6720 J=1,30
        I=35-J
      EL(I)=EL(I-1)-1.2192

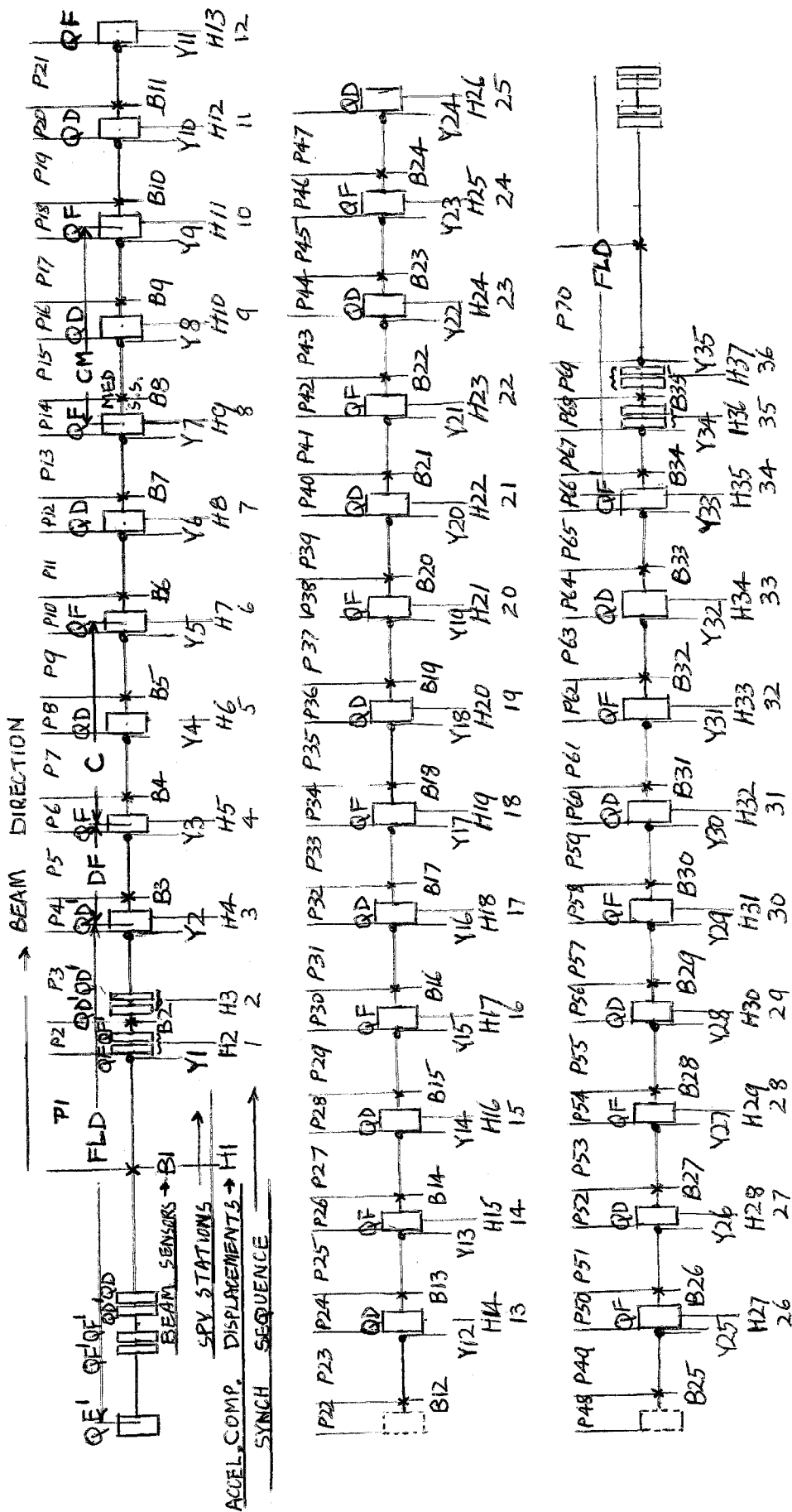
```

```

EL(4)=EL(3)-J*.812165
SM=EL(2)
EL(3)=SM+2.384045
EL(2)=SM-2.74358
DO 6730 J=1,5
DO 6730 I=1,37
6730 EL(I+J*37)=6283.1853*FLOAT(J)/6.+EL(I)
PRINT 6740, (EL(I),I=1,NH)
C GENERATE HARMONIC RESPONSE OF CLOSED ORBIT
DO 4000 I=1,NHAK
DO 4030 J=1,NFI
DO 4010 K=1,NH
H(K)=SIN(I*TP*EL(K)+TP*(J-1)/NFI)
DO 4020 L=1,NB
R(L)=0.
DO 4020 M=1,NH
B(L)=B(L)+S(L,M)*H(M)
CALL NUMBER(B,BMAX,IBMAX,BRMS,NB)
IB(J)=IBMAX
BM(J)=BMAX
BRM(J)=BRMS
CALL NUMBER (RM,BMMAX,IBMMAX,BMRMS,NFI)
CALL NUMBER (BRM,BRMMAX,IBRMMAX,BRMRMS,NFI)
PHM=J60.*(IBMMAX-1)/NFI
PHRM=360.*(IBRMMAX-1)/NFI
NM=IB(IBMMAX)
NRM=IB(IBRMMAX)
IF(I.NE.1) GO TO 4060
PRINT 4050
FORMAT (80H
HARMONIC MAX.AMPLITUDE PHASE MAX.R
1MS AMPLITUDE PHASE
4060 PRINT 4070,I,NM,BMMAX,PHM,NRM,BRMMAX,PHRM
4070 FORMAT (12X,13,1X,13,2X,E12.4,2X,F6.1,9X,13,2X,E12.4,2X,F5.1)
4080 CONTINUE
IF(NHOR.NE.1) GO TO 870
NHOR=1
IF(INVERT.EQ.1) GO TO 3020
CONTINUE
RETURN
END
SUBROUTINE NUMBER(C,CMAX,ICMAX,CRMS,NB)
DIMENSION C(222)
ICMAX=1
CMAX=ABS(C(1))
DO 30 I=2,NB
IF (ABS(C(I)).GT.CMAX) GO TO 20
GO TO 30
20 CMAX=ABS(C(I))
ICMAX=I
CONTINUE
30 CRMS=0.
DO 40 I=1,NB
CRMS=CMAX+C(I)**2/NB
40 CRMS=SQRT(CRMS)
RETURN
END
EOR 1 15. 10
EOF

```

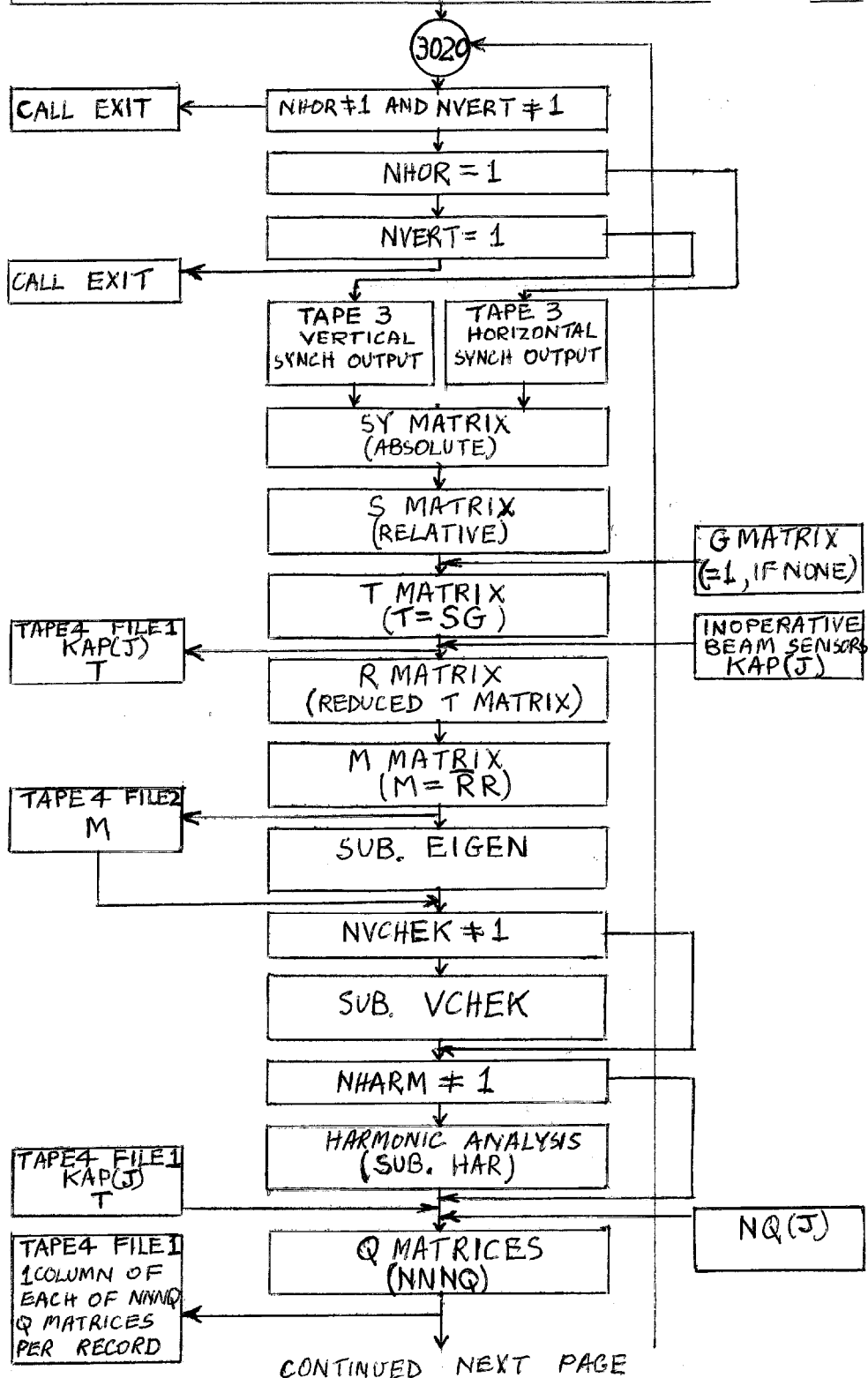




**FIG. 1** First superperiod of main ring showing locations of beam sensors, spy stations, accelerator component displacements. The displacement sequence used in SYNCH is also shown.

DATA

ITEST, ISPY, NHOR, NVERT, KAPUTH, KAPUTV, NVCHEK, NHARM, NNNQ (1615)  
 KAP(J) 1615  
 NQ(J) 1615 } HORIZONTAL  
 BS(J) 8F10.4  
 KAP(J) 1615  
 NQ(J) 1615 } VERTICAL  
 BS(J) 8F10.4



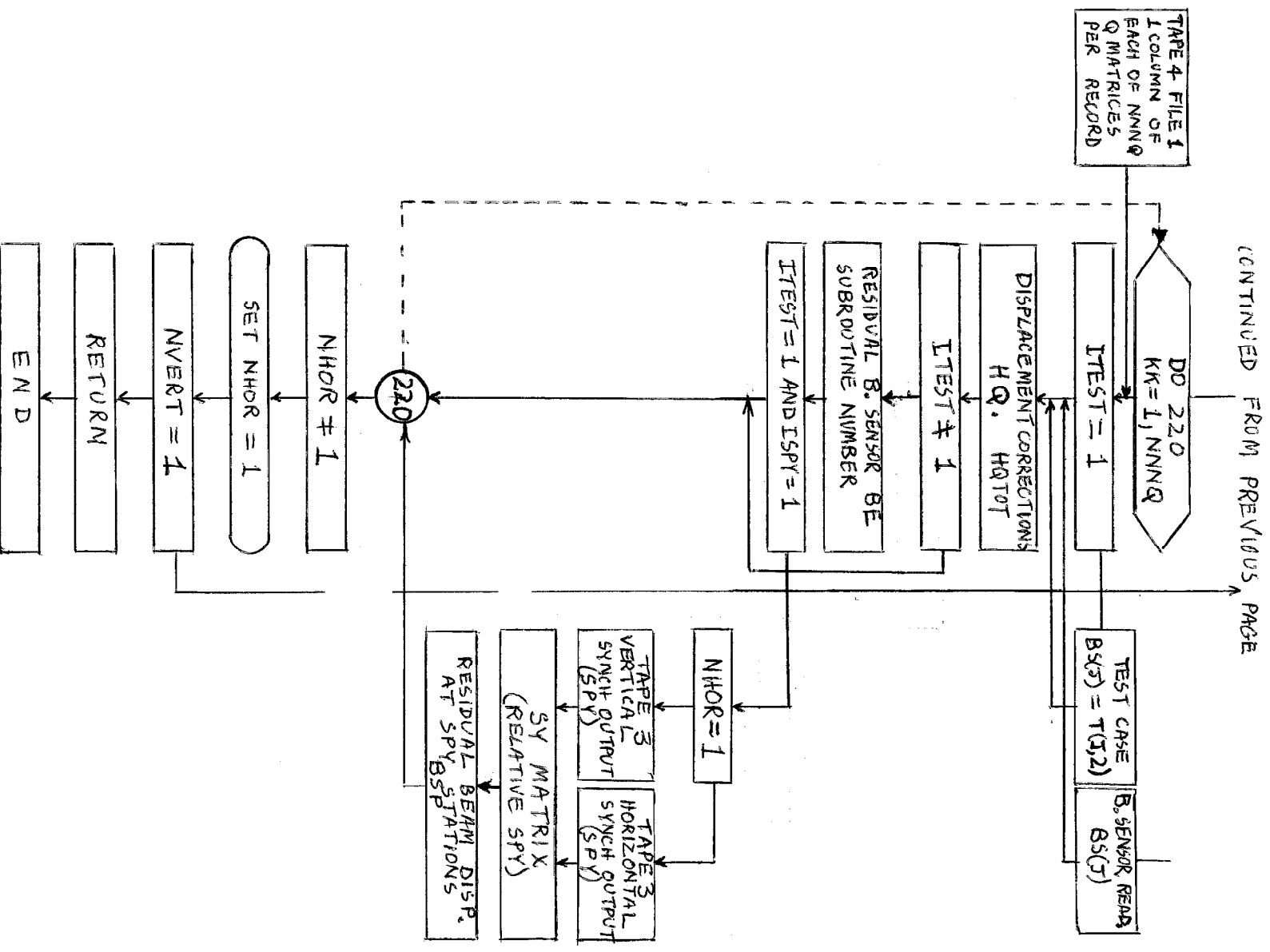


FIG. 2 Flow diagram for program OTRIM.

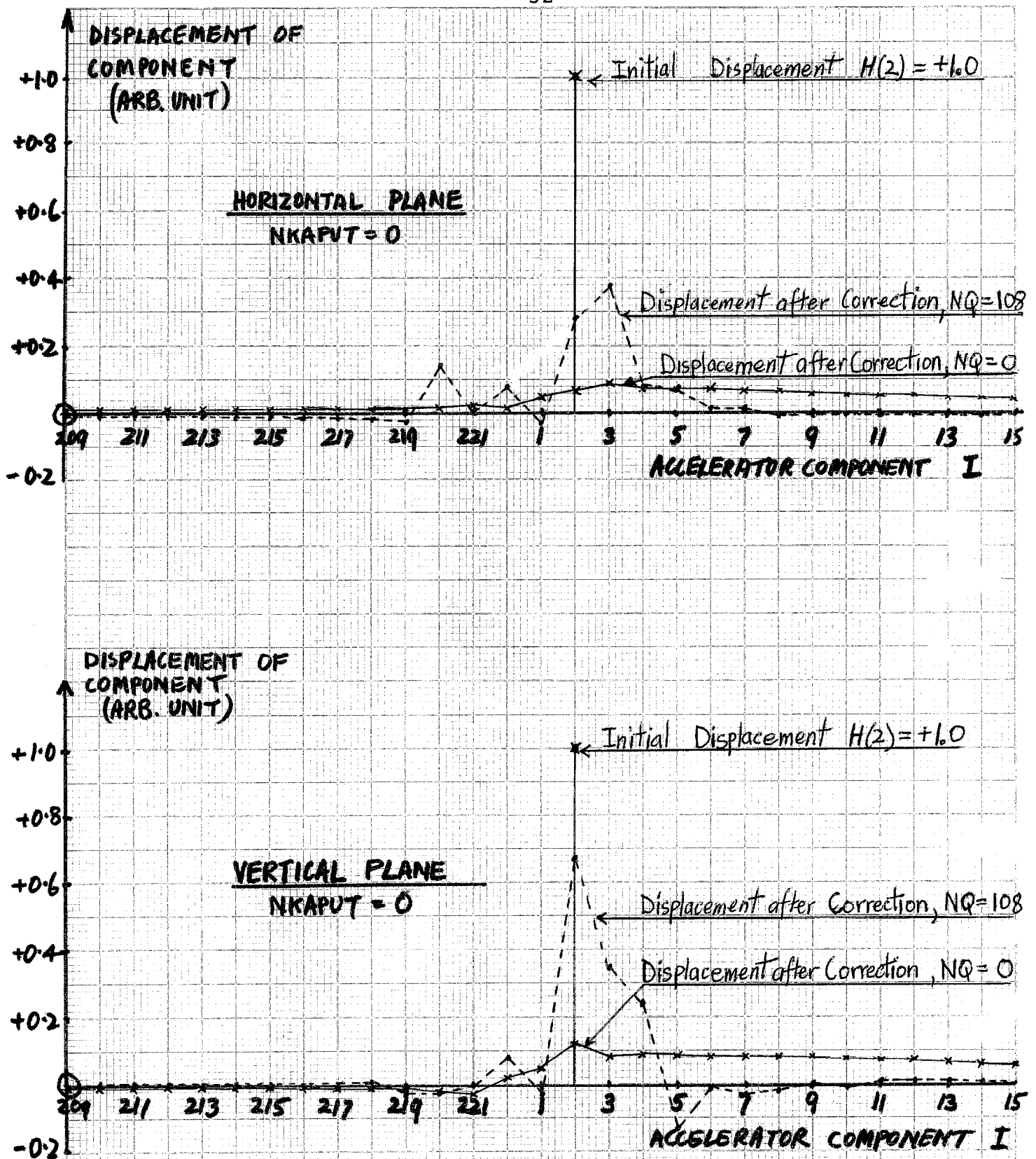
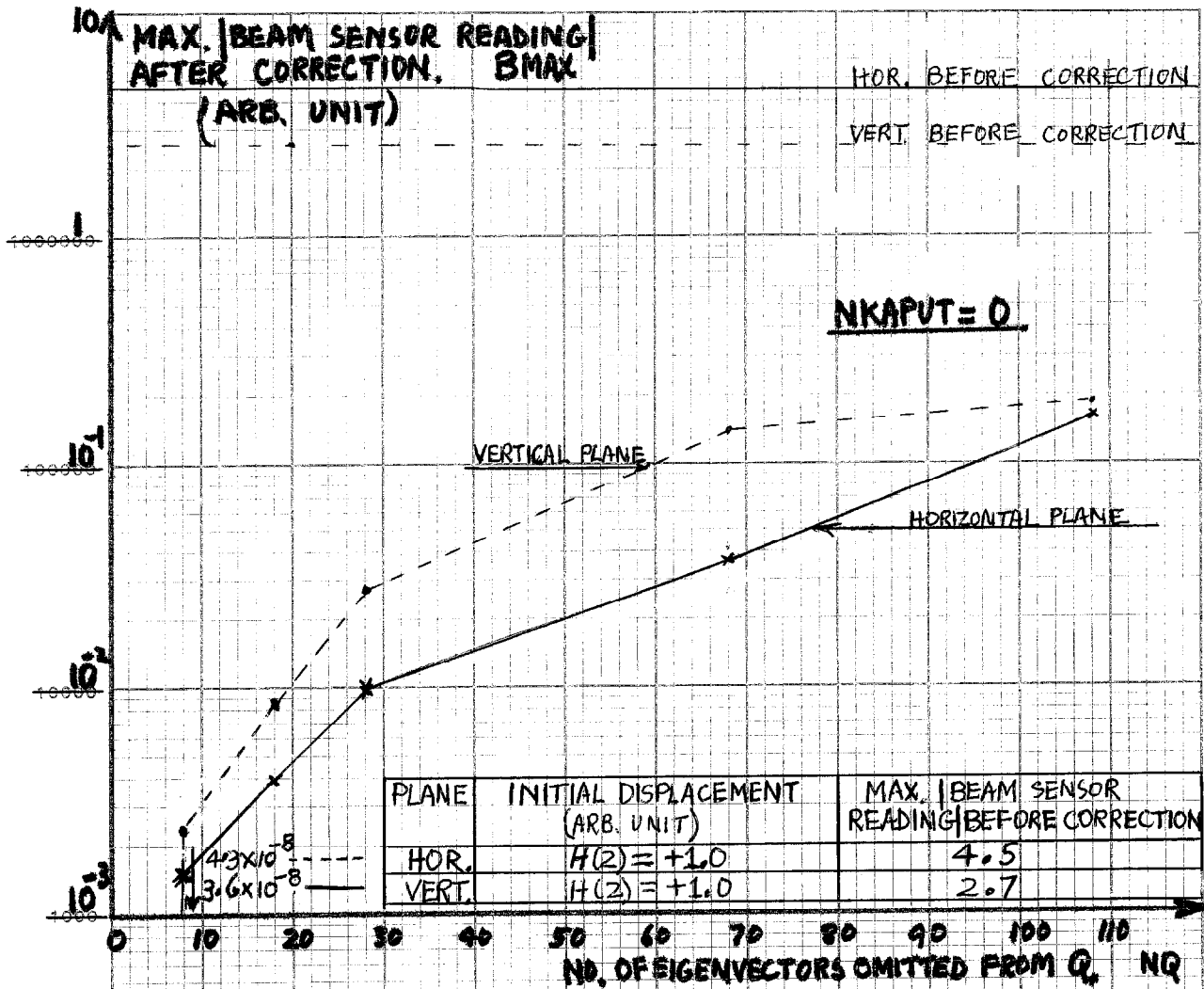
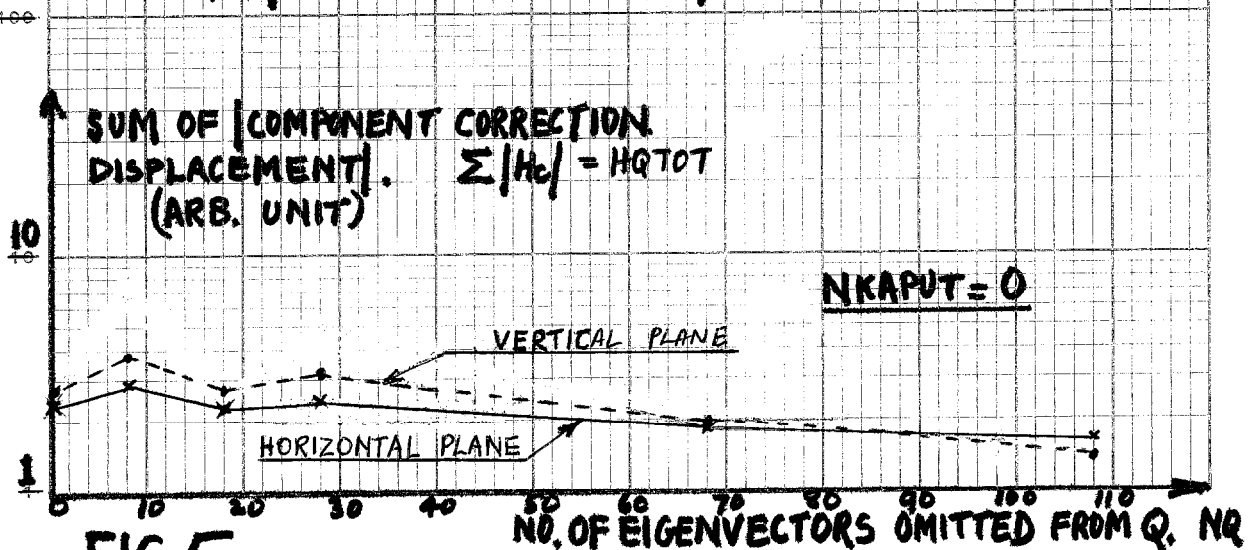


FIG. 3 Displacement of accelerator components before and after correction for case where all beam sensors are operative

DATE



**FIG. 4 EFFECT OF SMALL EIGENVALUE EIGENVECTOR OMISSION ON MAX. |BEAM SENSOR READING| AFTER CORRECTION.**



**FIG. 5 EFFECT OF SMALL EIGENVALUE EIGENVECTOR OMISSION ON SUM OF |COMPONENT CORRECTION DISPLACEMENT|.**

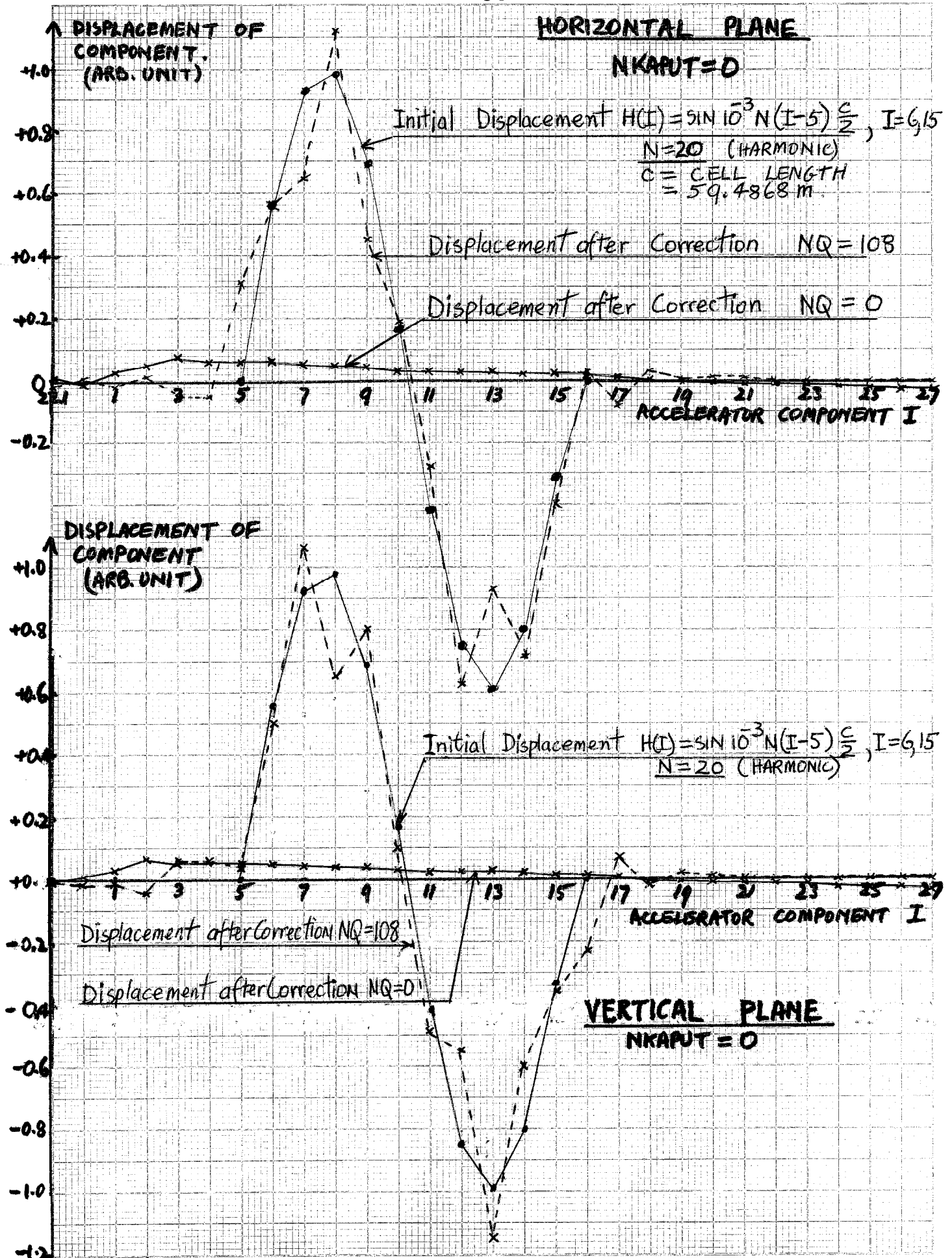


FIG.6 DISPLACEMENTS BEFORE AND AFTER CORRECTION. HARMONIC = 20

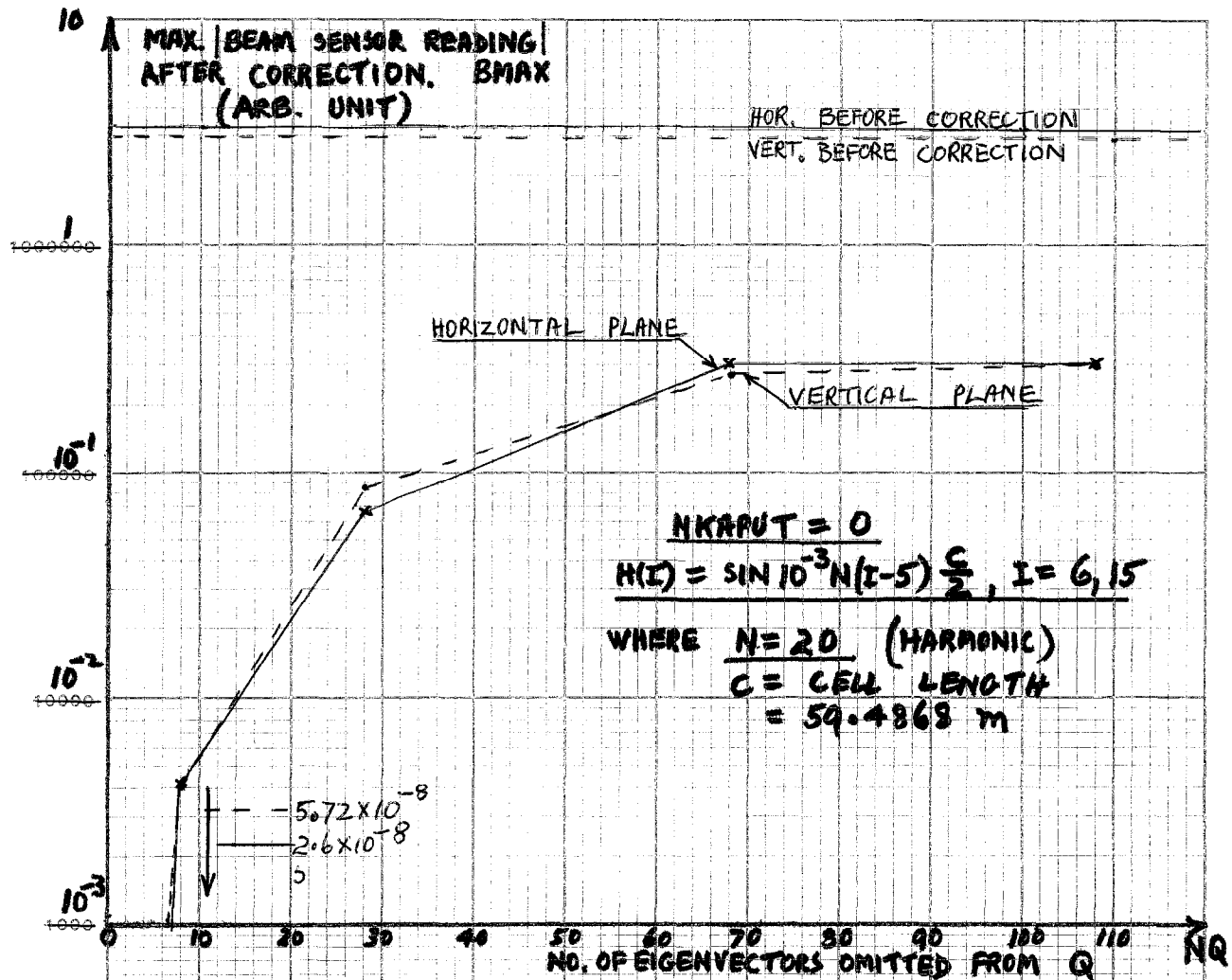


FIG. 7 EFFECT OF SMALL EIGENVALUE EIGENVECTOR OMISSION ON MAX. |BEAM SENSOR READING| AFTER CORRECTION

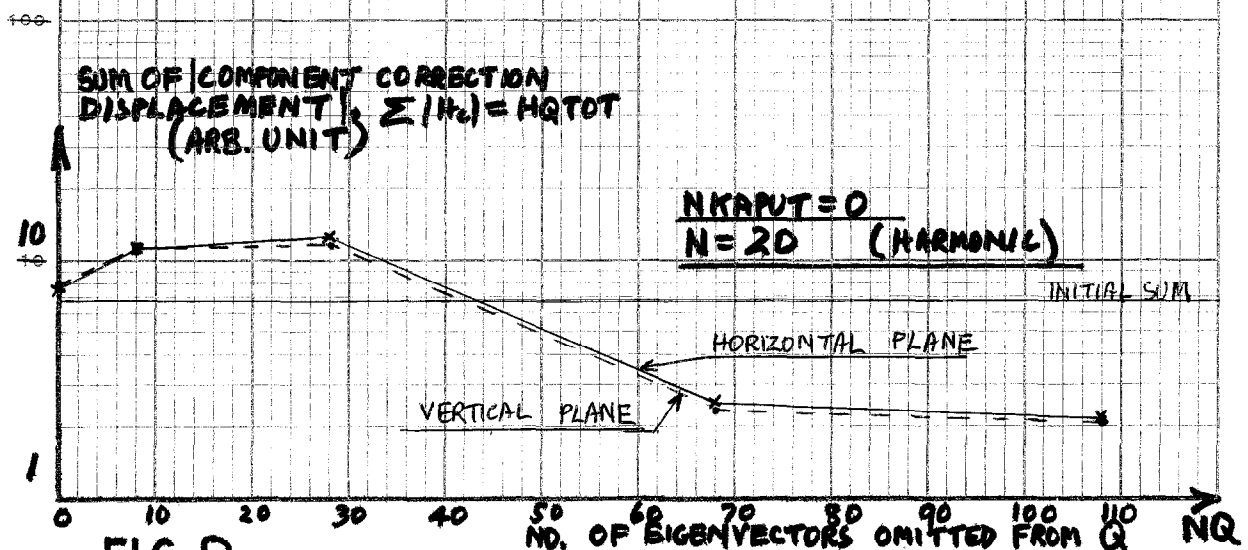


FIG. 8 EFFECT OF SMALL EIGENVALUE EIGENVECTOR OMISSION ON SUM OF COMPONENT CORRECTION DISPLACEMENT.

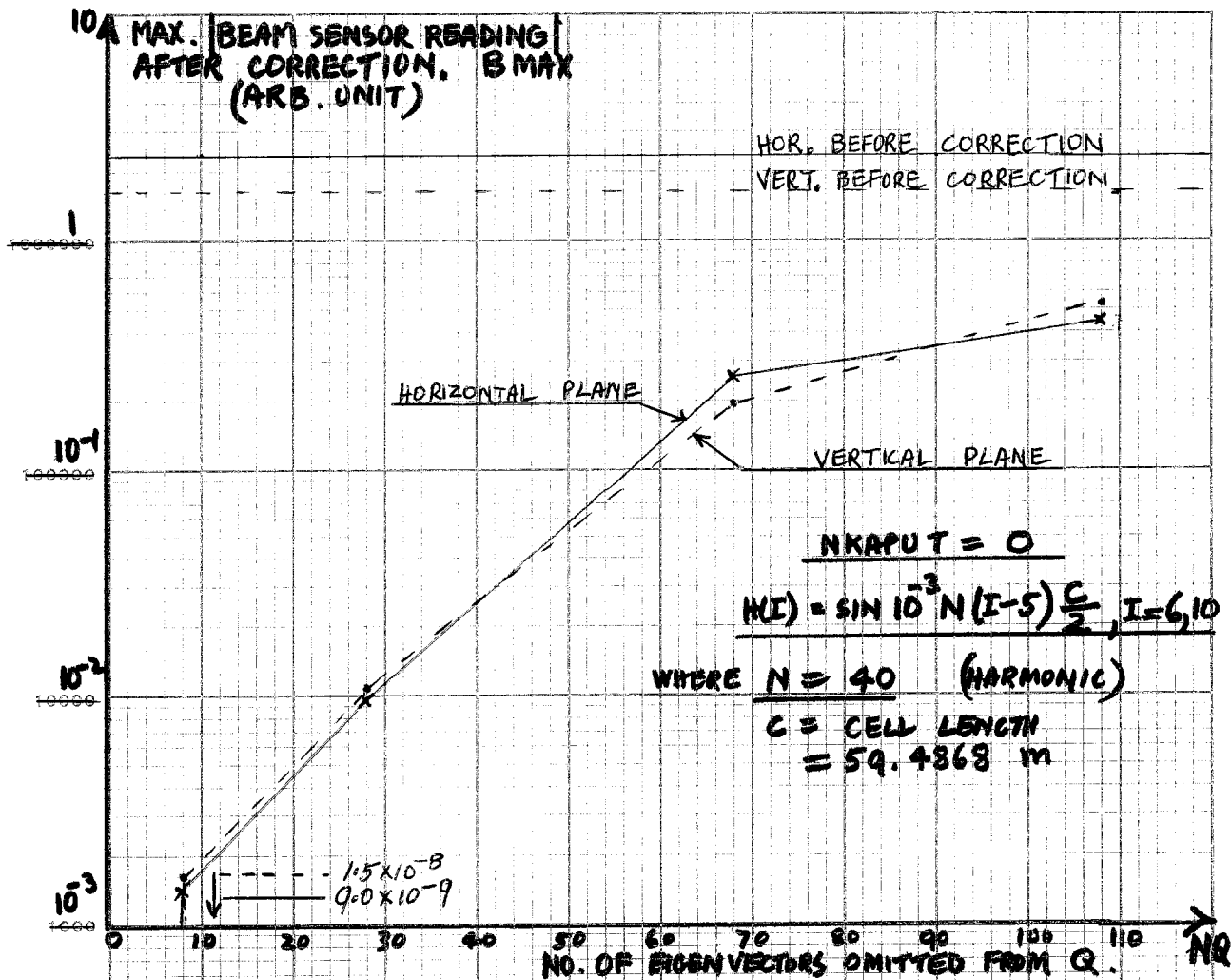


FIG. 9 EFFECT OF SMALL EIGENVALUE EIGENVECTOR OMISSION ON MAX. |BEAM SENSOR READING| AFTER CORRECTION.

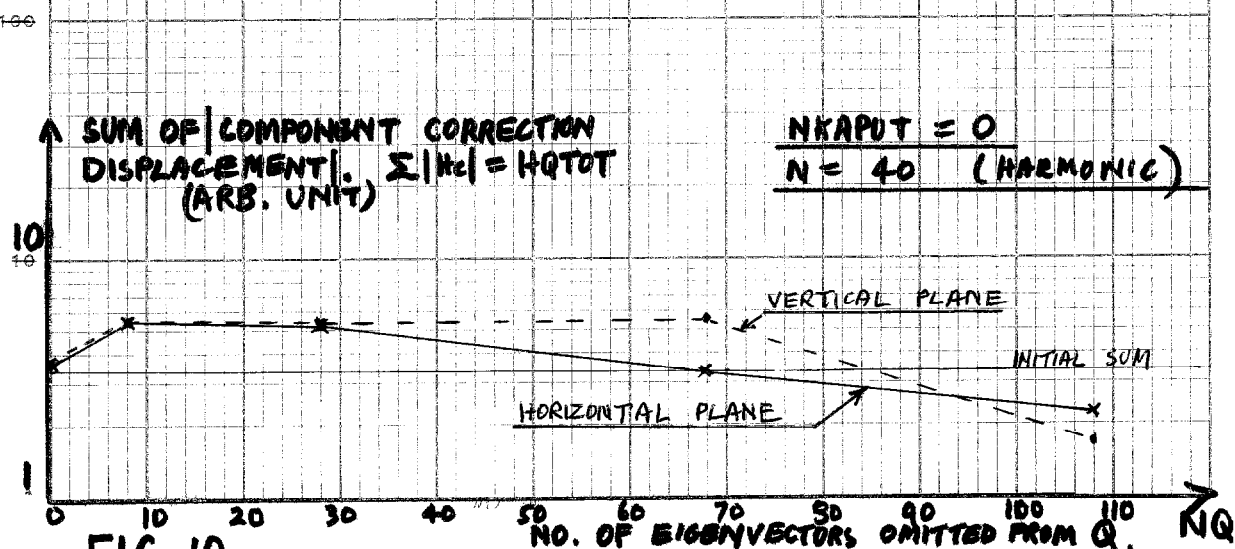
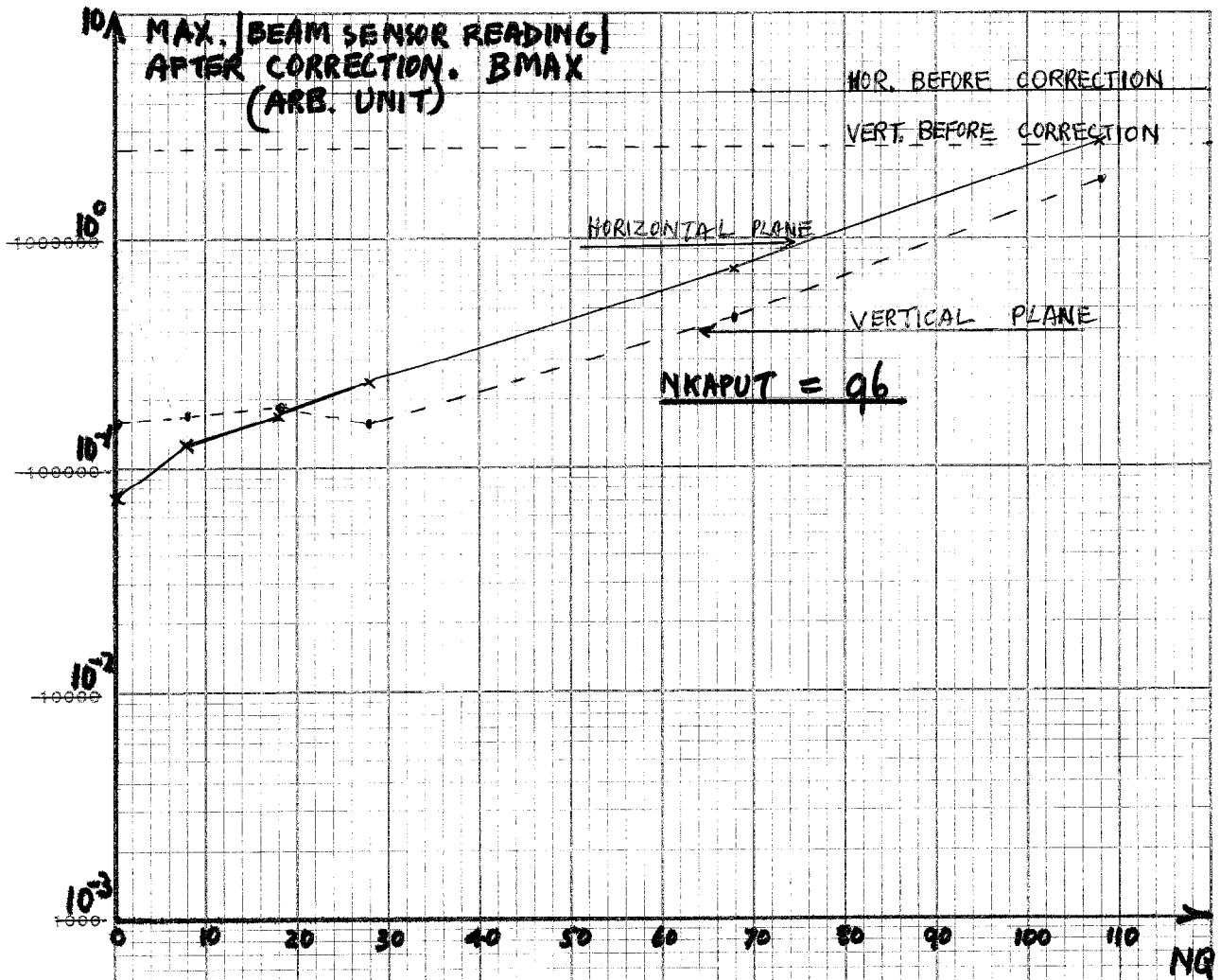
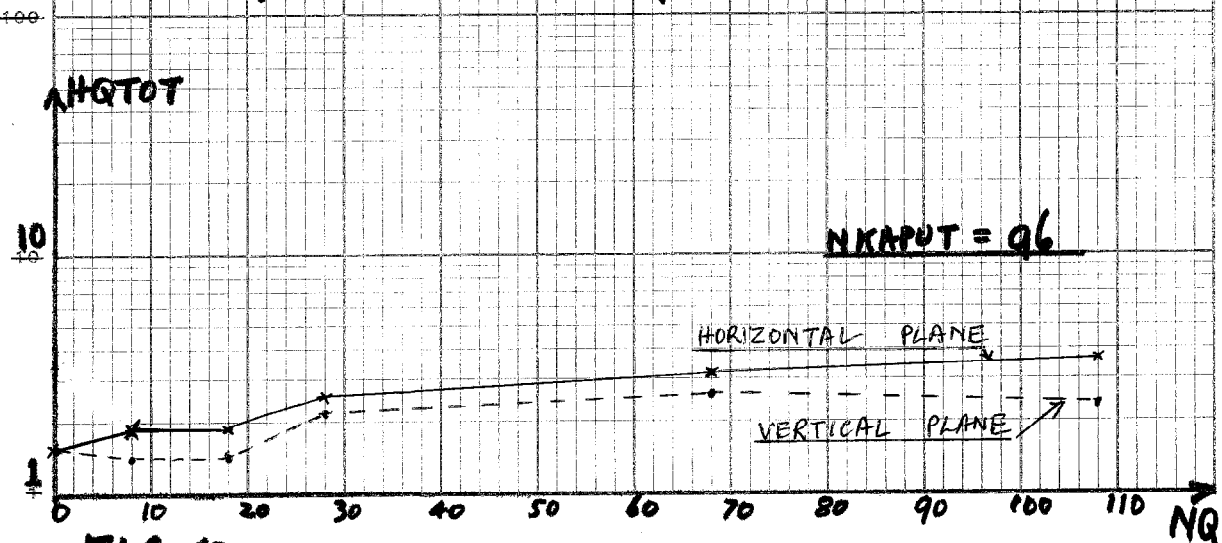


FIG. 10 EFFECT OF SMALL EIGENVALUE EIGENVECTOR OMISSION ON SUM OF |COMPONENT CORRECTION DISPLACEMENT|.

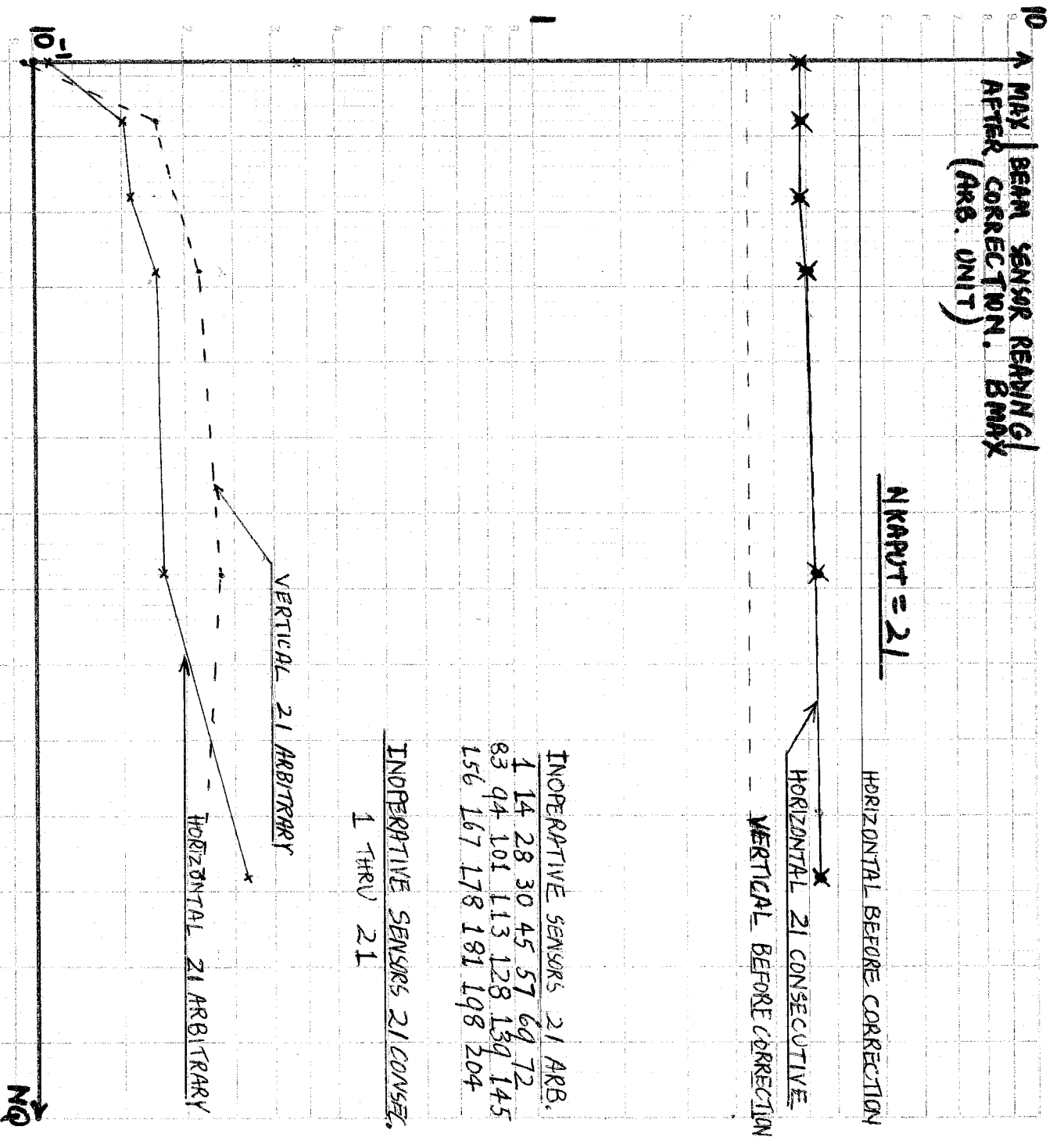




**FIG. 11** EFFECT OF SMALL EIGENVALUE EIGENVECTOR OMISSION ON MAX. |BEAM SENSOR READING| AFTER CORRECTION.  $NKAPUT=96$

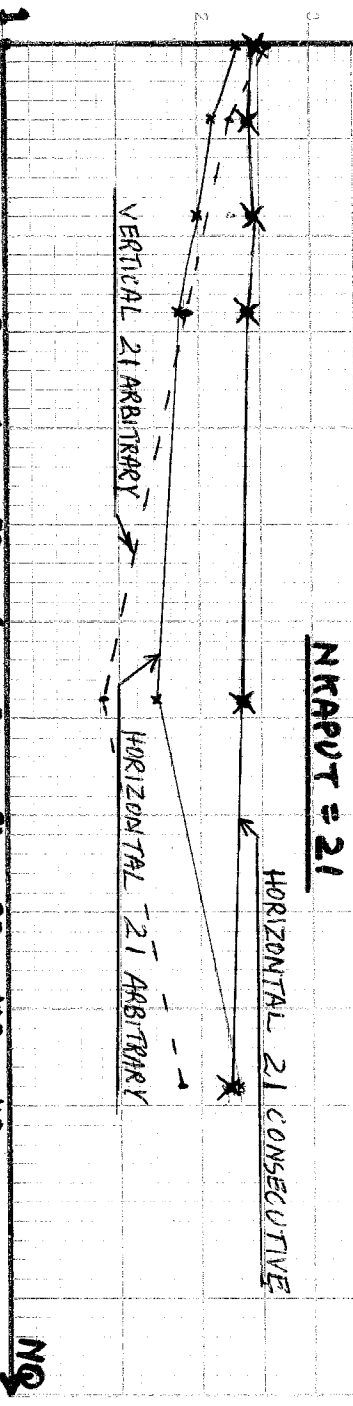


**FIG. 12** EFFECT OF SMALL EIGENVALUE EIGENVECTOR OMISSION ON SUM OF |COMPONENT CORRECTION DISPLACEMENT|.  $NKAPUT=96$



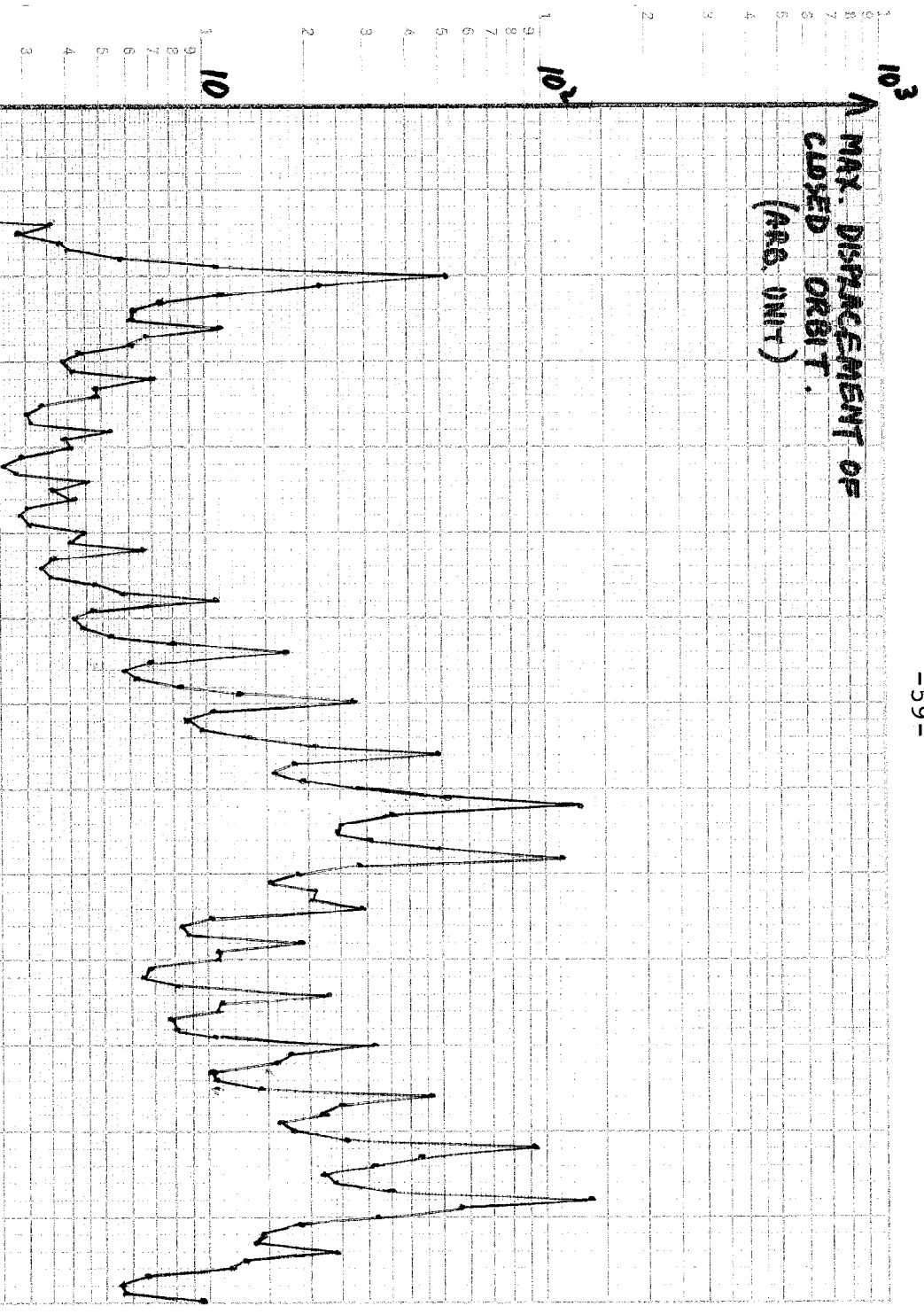
**FIG 13 EFFECT OF SMALL EIGENVALUE EIGENVECTOR OMISSION ON  
BMAX FOR NKAPUT = 21 CASES SHOWN.**

**ΔHOTOT = Σ |COMPONENT CORRECTION DISPLACEMENT|**



**FIG 14 EFFECT OF NQ ON HOTOT FOR NKAPUT = 21 CASES SHOWN**

Δ MAX. DISPLACEMENT OF  
CLOSED ORBIT.  
(ARB. UNIT)



HORIZONTAL PLANE

ACCELERATOR COMPONENTS DISPLACED  
ACCORDING TO HARMONIC WITH  
AMPLITUDE = 1 ARB. UNIT

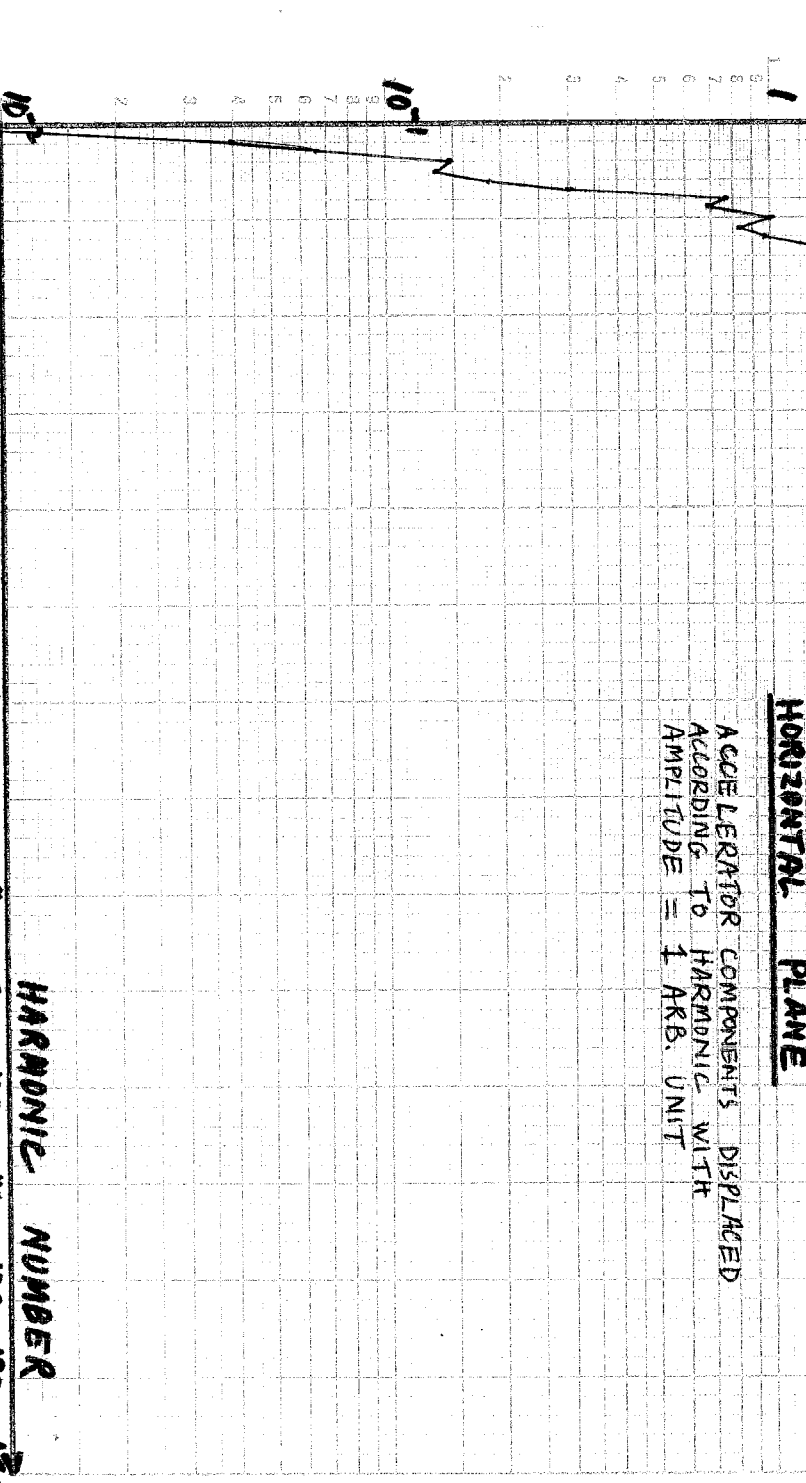
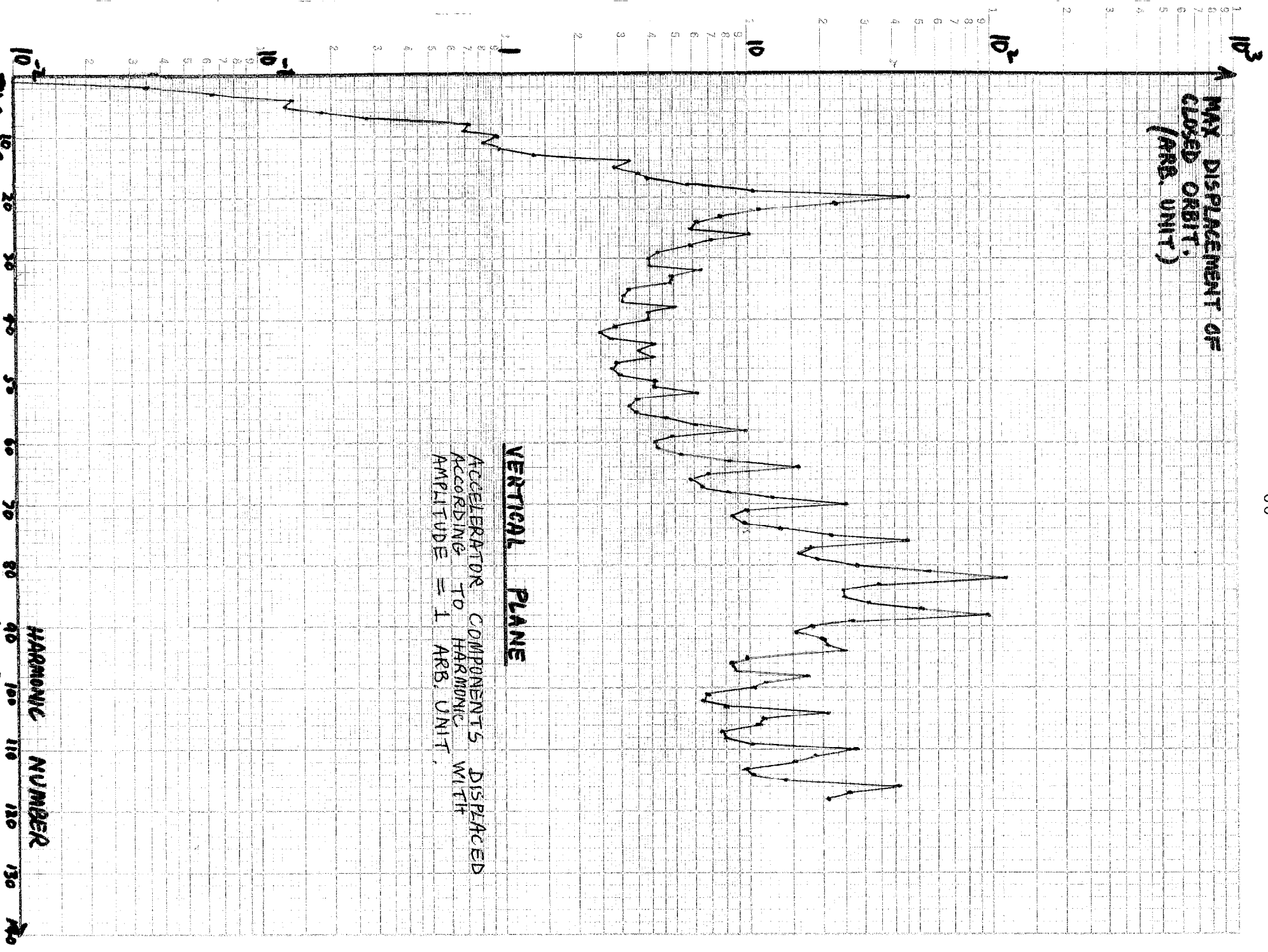


FIG. 15 HARMONIC RESPONSE IN HORIZONTAL PLANE.



**FIG. 16 HARMONIC RESPONSE IN VERTICAL PLANE.**